



Smart Analytics for Big Time-series Data

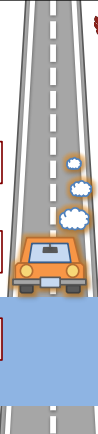
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Roadmap

- Motivation
- Similarity search, pattern discovery and summarization Part 1
- Non-linear modeling and forecasting Part 2
- **Extension of time-series data: tensor analysis** Part 3



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Part 3

Extension of time-series: tensor analysis

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Outline

- ➔ Tensor decomposition
 - Mining and forecasting of complex time-stamped events
 - New challenge: MANT analysis

Multi-Aspect Non-linear Time-series




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Outline

- Tensor decomposition
- ➔ - Motivation
- Basic approaches
- Mining and forecasting of complex time-stamped events
- New challenge: MANT analysis

Multi-Aspect Non-linear Time-series



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Examples of Matrices: Graph - social network

	John	Peter	Mary	Nick	...
John	0	11	22	55	...
Peter	5	0	6	7	...
Mary
Nick
...

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Examples of Matrices:
cloud of n-dim points

	chol#	blood#	age
John	13	11	22	55	...
Peter	5	4	6	7	...
Mary
Nick
...

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Examples of Matrices:
Market basket

- market basket as in Association Rules

	milk	bread	choc.	wine	...
John	13	11	22	55	...
Peter	5	4	6	7	...
Mary
Nick
...

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Examples of Matrices:
Documents and terms

	data	mining	classif.	tree	...
Paper#1	13	11	22	55	...
Paper#2	5	4	6	7	...
Paper#3
Paper#4
...

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Examples of Matrices:
Authors and terms

	data	mining	classif.	tree	...
John	13	11	22	55	...
Peter	5	4	6	7	...
Mary
Nick
...

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Examples of Matrices:
sensor-ids and time-ticks

	temp1	temp2	humid.	pressure	...
t=1	13	11	22	55	...
t=2	5	4	6	7	...
t=3
t=4
...

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Motivation 2: Why tensors?

- Q: what is a tensor?
- A: N-D generalization of matrix:

	network	search	graph	mining	...
John	13	11	22	55	...
Peter	5	4	6	7	...
Mary
Nick
...

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Motivation 2: Why tensors?

- Q: what is a tensor?
- A: N-D generalization of matrix:

kdd' 15
 kdd' 16
 kdd' 17
 network search graph mining ...
 John 13 11 22 55 ...
 Peter 5 4 6 7 ...
 Mary
 Nick

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Tensors are useful for 3 or more modes

Terminology: 'mode' (or 'aspect'):

Mode#3
 Mode#2
 Mode (= aspect) #1

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Motivating Applications

- Why tensors are useful?
 - P1: social networks
 - P2: web mining

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P1: Social network analysis

- Monitoring networks and community structures over time

2004 Keywords
 1990 Authors

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P2: Web graph mining

- How to order the importance of web pages?
 - Kleinberg's algorithm HITS
 - PageRank
 - Tensor extension on HITS (TOPHITS)
 - context-sensitive hypergraph analysis

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Tensor analysis for time-series data

- Time-stamped events
 - e.g., web clicks

Time	URL	User
08-01-12:00	CNN.com	Smith
08-02-15:00	YouTube.com	Brown
08-02-19:00	CNET.com	Smith
08-03-11:00	CNN.com	Johnson
...

URL u
 user v
 n Time

Represent as M^{th} order tensor ($M=3$)
 $\mathcal{X} \in \mathbb{N}^{u \times v \times n}$

Element x: # of events

e.g., 'Smith', 'CNN.com', 'Aug 1, 10pm'; 21 times

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Tensor analysis for time-series data

- Individual-sequence mining
 - Create a set of $(u * v)$ sequences of length (n)
 - Apply the mining algorithm for each sequence

URL u
user v
 n
time

u
 v
 n

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Tensor analysis for time-series data

- Multi-aspect time-series analysis

URL u
user v
 n
time
Web clicks \mathcal{X}

URL
time
Topic A (business)
Topic B (news)
Topic C (media)

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Outline

- Tensor decomposition
 - Motivation
 - Basic approaches
- Mining and forecasting of complex time-stamped events
- New challenge: MANT analysis

Multi-Aspect Non-linear Time-series

M A N T

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Reminder: SVD

$$A \approx U \Sigma V^T = \sum_i \sigma_i \mathbf{u}_i \circ \mathbf{v}_i$$

m n
 A
 m n
 Σ V^T
 U

– Best rank-k approximation in L2

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Reminder: SVD

$$A \approx U \Sigma V^T = \sum_i \sigma_i \mathbf{u}_i \circ \mathbf{v}_i$$

m n
 A
 $\sigma_1 \mathbf{u}_1 \circ \mathbf{v}_1$
 $\sigma_2 \mathbf{u}_2 \circ \mathbf{v}_2$

– Best rank-k approximation in L2

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Goal: extension to ≥ 3 modes

$I \times J \times K$
 \mathcal{X}
 $I \times R$ $R \times R \times R$ $J \times R$
 A B C
 λ
 $= \lambda_1 \dots + \lambda_R$

$$\mathcal{X} \approx [\lambda ; A, B, C] = \sum_r \lambda_r \mathbf{a}_r \circ \mathbf{b}_r \circ \mathbf{c}_r$$

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Main points:

- 2 major types of tensor decompositions: PARAFAC and Tucker
- both can be solved with "alternating least squares" (ALS)

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Specially Structured Tensors

Tucker Tensor

$$\mathcal{X} = \mathcal{G} \times_1 \mathbf{U} \times_2 \mathbf{V} \times_3 \mathbf{W}$$

$$= \sum_r \sum_s \sum_t g_{rst} \mathbf{u}_r \circ \mathbf{v}_s \circ \mathbf{w}_t$$

$$\equiv [\mathcal{G}; \mathbf{U}, \mathbf{V}, \mathbf{W}]$$

Our Notation

Kruskal Tensor

$$\mathcal{X} = \sum_r \lambda_r \mathbf{u}_r \circ \mathbf{v}_r \circ \mathbf{w}_r$$

$$\equiv [\lambda; \mathbf{U}, \mathbf{V}, \mathbf{W}]$$

Our Notation

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Specially Structured Tensors

Tucker Tensor

$$\mathcal{X} = \mathcal{G} \times_1 \mathbf{U} \times_2 \mathbf{V} \times_3 \mathbf{W}$$

$$= \sum_r \sum_s \sum_t g_{rst} \mathbf{u}_r \circ \mathbf{v}_s \circ \mathbf{w}_t$$

$$\equiv [\mathcal{G}; \mathbf{U}, \mathbf{V}, \mathbf{W}]$$

In matrix form:

$$\mathbf{X}_{(1)} = \mathbf{U} \mathbf{G}_{(1)} (\mathbf{W} \otimes \mathbf{V})^T$$

$$\mathbf{X}_{(2)} = \mathbf{V} \mathbf{G}_{(2)} (\mathbf{W} \otimes \mathbf{U})^T$$

$$\mathbf{X}_{(3)} = \mathbf{W} \mathbf{G}_{(3)} (\mathbf{V} \otimes \mathbf{U})^T$$

$$\text{vec}(\mathcal{X}) = (\mathbf{W} \otimes \mathbf{V} \otimes \mathbf{U}) \text{vec}(\mathcal{G})$$

Kruskal Tensor

$$\mathcal{X} = \sum_r \lambda_r \mathbf{u}_r \circ \mathbf{v}_r \circ \mathbf{w}_r$$

$$\equiv [\lambda; \mathbf{U}, \mathbf{V}, \mathbf{W}]$$

In matrix form:

Let $\Lambda = \text{diag}(\lambda)$

$$\mathbf{X}_{(1)} = \mathbf{U} \Lambda (\mathbf{W} \odot \mathbf{V})^T$$

$$\mathbf{X}_{(2)} = \mathbf{V} \Lambda (\mathbf{W} \odot \mathbf{U})^T$$

$$\mathbf{X}_{(3)} = \mathbf{W} \Lambda (\mathbf{V} \odot \mathbf{U})^T$$

$$\text{vec}(\mathcal{X}) = (\mathbf{W} \odot \mathbf{V} \odot \mathbf{U}) \lambda$$

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Tucker Decomposition - intuition

- author x keyword x conference
- A: author x author-group
- B: keyword x keyword-group
- C: conf. x conf-group
- G: how groups relate to each other

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Intuition behind core tensor

- 2-d case: co-clustering
- [Dhillon et al. Information-Theoretic Co-clustering, KDD' 03]

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Intuition behind core tensor

eg, terms x documents

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med. doc cs doc

term group x doc. group

med. terms
cs terms
common terms

$$\begin{bmatrix} .05 & .05 & 0 & 0 & 0 \\ .05 & .05 & 0 & 0 & 0 \\ 0 & 0 & .05 & .05 & .05 \\ 0 & 0 & .05 & .05 & .05 \\ .04 & .04 & 0 & .04 & .04 \\ .04 & .04 & 0 & .04 & .04 \end{bmatrix} \begin{bmatrix} 3 & 0 \\ 0 & 3 \\ 2 & 2 \end{bmatrix} = \begin{bmatrix} .054 & .054 & .042 & 0 & 0 & 0 \\ .054 & .054 & .042 & 0 & 0 & 0 \\ 0 & 0 & 0 & .042 & .054 & .054 \\ 0 & 0 & 0 & .042 & .054 & .054 \\ .036 & .036 & .028 & .028 & .036 & .036 \\ .036 & .036 & .028 & .028 & .036 & .036 \end{bmatrix}$$

doc x doc group

term x term-group

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Tucker Decomposition

$\mathcal{X} \approx [\mathcal{G}; A, B, C]$

Given A, B, C, the optimal core is:
 $\mathcal{G} = [\mathcal{X}; A^\dagger, B^\dagger, C^\dagger]$

Recall the equations for converting a tensor to a matrix

$$\begin{aligned} X_{(1)} &= A G_{(1)} (C \otimes B)^\top \\ X_{(2)} &= B G_{(2)} (C \otimes A)^\top \\ X_{(3)} &= C G_{(3)} (B \otimes A)^\top \\ \text{vec}(\mathcal{X}) &= (C \otimes B \otimes A) \text{vec}(\mathcal{G}) \end{aligned}$$

- Proposed by Tucker (1966)
- AKA: Three-mode factor analysis, three-mode PCA, orthogonal array decomposition
- A, B, and C generally assumed to be orthonormal (generally assume they have full column rank)
- \mathcal{G} is not diagonal
- Not unique

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CANDECOMP/PARAFAC Decomposition

$\mathcal{X} \approx [\lambda; A, B, C] = \sum_r \lambda_r a_r \circ b_r \circ c_r$

- CANDECOMP = Canonical Decomposition (Carroll & Chang, 1970)
- PARAFAC = Parallel Factors (Harshman, 1970)
- Core is diagonal (specified by the vector λ)
- Columns of A, B, and C are not orthonormal
- If R is minimal, then R is called the **rank** of the tensor (Kruskal 1977)
- Can have $\text{rank}(\cdot) > \min\{I, J, K\}$

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Tucker vs. PARAFAC Decompositions

- Tucker**
 - Variable transformation in each mode
 - Core G may be dense
 - A, B, C generally orthonormal
 - Not unique
- PARAFAC**
 - Sum of rank-1 components
 - No core, i.e., superdiagonal core
 - A, B, C may have linearly dependent columns
 - Generally unique

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Tensor tools - summary

- Two main tools
 - PARAFAC
 - Tucker
- Both find row-, column-, tube-groups
 - but in PARAFAC the three groups are identical
- To solve: Alternating Least Squares
- Toolbox: from Tamara Kolda: <http://csmr.ca.sandia.gov/~tgkolda/TensorToolbox/>

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Outline

- Tensor decomposition
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- New challenge: MANT analysis

Multi-Aspect Non-linear Time-series

MANT

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[Matsubara+ KDD'12]



Fast Mining and Forecasting of Complex Time-Stamped Events

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 Yasushi Sakurai (NTT)
 Christos Faloutsos (CMU)
 Tomoharu Iwata (NTT)
 Masatoshi Yoshikawa (Kyoto University)



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Motivation

- Complex time-stamped events
{timestamp + multiple attributes}

e.g., web click events:
{timestamp, URL, user ID, access devices, http referrer,...}

Timestamp	URL	User	Device
2012-08-01-12:00	CNN.com	Smith	iphone
2012-08-02-15:00	YouTube.com	Brown	iphone
2012-08-02-19:00	CNET.com	Smith	mac
2012-08-03-11:00	CNN.com	Johnson	ipad
...

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Motivation

Q1. Are there any topics ?

- news, tech, media, sports, etc...

Timestamp	URL	User	Device
2012-08-01-12:00	CNN.com	Smith	iphone
2012-08-02-15:00	YouTube.com	Brown	iphone
2012-08-02-19:00	CNET.com	Smith	mac
2012-08-03-11:00	CNN.com	Johnson	ipad
...

e.g.,

- CNN.com, CNET.com → news topic
- YouTube.com → media topic



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Motivation

Q2. Can we group URLs/users accordingly?

Timestamp	URL	User	Device
2012-08-01-12:00	CNN.com	Smith	iphone
2012-08-02-15:00	YouTube.com	Brown	iphone
2012-08-02-19:00	CNET.com	Smith	mac
2012-08-03-11:00	CNN.com	Johnson	ipad
...

e.g.,

- CNN.com & CNET.com (related to news topic)
- Smith & Johnson (related to news topic)



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Motivation

Q3. Can we forecast future events?

- How many clicks from 'Smith' tomorrow?
- How many clicks to 'CNN.com' over next 7 days?

Timestamp	URL	User	Device
2012-08-01-12:00	CNN.com	Smith	iphone
2012-08-02-15:00	YouTube.com	Brown	iphone
2012-08-02-19:00	CNET.com	Smith	mac
2012-08-03-11:00	CNN.com	Johnson	ipad
2012-08-05-12:00	CNN.com	Smith	iphone
2012-08-05-19:00	CNET.com	Smith	iphone

future clicks?

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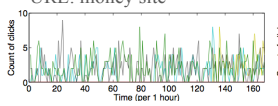
Motivation

Web click events – can we see any trends?

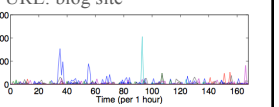
Original access counts of each URL

- 100 random users
- 1 week (window size = 1 hour)

URL: money site



URL: blog site



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Motivation

Web click events – can we see any trends?
Original access counts of each URL

⊗ **Noisy** users
⊗ **Sparse** window size
⊗ **Bursty**

URL: movie site URL: blog site

Count of clicks vs Time (per 1 hour)

⊗ **We cannot see any trends !!**

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Our goals

Q1: Hidden topics → business news media
Q2: Groups → Groups
Q3: Forecasting → Events ?

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Problem definition

Given: a set of complex time-stamped events
1. Find: major topics/trends
2. Forecast: future events

Original web-click events → URL in topic space → User in topic space

“Hidden topics” wrt each aspect (URL, user, time)

Time evolution

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Main idea (1) : M-way analysis

Complex time-stamped events
e.g., web clicks

Time	URL	User
08-01-12:00	CNN.com	Smith
08-02-15:00	YouTube.com	Brown
08-02-19:00	CNET.com	Smith
08-03-11:00	CNN.com	Johnson
...

object/URL u
actor/user v
Time n

Element x : # of events
e.g., ‘Smith’, ‘CNN.com’, ‘Aug 1, 10pm’; 21 times

Represent as M^{th} order tensor ($M=3$)
 $\mathcal{X} \in \mathbb{N}^{u \times v \times n}$

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Main idea (1) : M-way analysis

A. decompose to a set of 3 topic vectors:

- Object vector (URL)
- Actor vector (user)
- Time vector (Time)

Web clicks \mathcal{X} = Topic A (business) + Topic B (news) + Topic C (media) + ...

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Main idea (1) : M-way analysis

A. decompose to a set of 3 topic vectors:

- Object vector (URL)
- Actor vector (user)
- Time vector (Time)

e.g., Business topic vectors

Higher value: Highly related topic

Object/URL: Money.com, CNN.com
Actor/user: Smith, Johnson
Time: Mon-Fri, Sat-Sun

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Main idea (1) : M-way analysis (details)

- M-way decomposition (M=3)
 - [Gibbs sampling] infer k hidden topics for each non-zero element of X, according to probability p

$$p(z_{i,j,t}) = r | \chi, O', A', C', \alpha, \beta, \gamma \quad (1)$$

$$\propto \frac{o'_{i,r} + \alpha}{\sum_r o'_{i,r} + \alpha k} \cdot \frac{a'_{r,j} + \beta}{\sum_j a'_{r,j} + \beta v} \cdot \frac{c'_{r,t} + \gamma}{\sum_t c'_{r,t} + \gamma n}$$

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Main idea (2) : Multi-scale analysis (details)

- Tensors with multiple window sizes

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Main idea (2) : Multi-scale analysis (details)

- Tensors with multiple window sizes

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TriMine-Forecasts

Our final goal: “forecast future events”!

Q. How can we generate a realistic events?

e.g., estimate the number of clicks for user “smith”, to URL “CNN.com”, for next 10 days

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Why not naïve?

- Individual-sequence forecasting
 - Create a set of (u * v) sequences of length (n)
 - Apply the forecasting algorithm for each sequence

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Why not naïve?

- Individual-sequence forecasting
 - Create a set of (u * v) sequences of length (n)
 - Apply the forecasting algorithm for each sequence

- ⊗ **Scalability** : time complexity is at least $O(uvn)$
- ⊗ **Accuracy** : each sequence “looks” like noise, (e.g., {0, 0, 0, 1, 0, 0, 2, 0, 0, ...}) -> hard to forecast

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TriMine-F

Our approach:

- Step 1: Forecast time-topic matrix:
- Step 2: Generate events using 3 matrices

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Forecast 'time-topic matrix' (details)

Q. How to capture multi-scale dynamics ?
e.g., bursty pattern, noise, multi-scale period

Multi-scale forecasting
Forecast $\hat{C}_{r,t}^{(0)}$ using multiple levels of matrices

$$C_{r,t}^{(0)} = \sum_{h=0}^{\lceil \log n \rceil} \sum_{i=1}^n \lambda_{i,r}^{(h)} C_{r,t-i}^{(h)} + \epsilon_t$$

(Details in paper)

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Our goals

- Q1: Hidden topics → business, news, media
- Q2: Groups → Groups
- Q3: Forecasting → Events

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Q1&2. WebClick data

URL-topic matrix (O)

Three hidden topics: "drive", "business", "media"

* Red point : each web site

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Q1&2. WebClick data

User-topic matrix (A)

Three hidden topics: "drive", "business", "media"

* Red point : each user

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Q1&2. WebClick data

Time-topic matrix (C)

Three hidden topics: "drive", "business", "media"

* Each sequence: each topic over time

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Q3. Forecasting accuracy

- Benefit of multiple time-scale forecasting

Original sequence of matrix (C)

Forecast C' using single level -> failed

Multi-scale forecast -> captured cyclic patterns

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Q3. Forecasting accuracy

Temporal perplexity (entropy for each time-tick)

Lower perplexity: higher predictive accuracy

(a) WebClick

(b) Ondemand TV T2: [Hong et al. KDD'11]

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Q3. Forecasting accuracy

Accuracy of event forecasting

RMSE between original and forecasted events (lower is better)

PLiF [Li et al. VLDB'10], T2: [Hong et al. KDD'11]

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Q3. Scalability

- Computation cost (vs. AR)

- TriMine provides a reduction in computation time (up to 74x)

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Outline

- Tensor decomposition
- Mining and forecasting of complex time-stamped events
- New challenge: MANT analysis

Multi-Aspect Non-linear Time-series

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Non-linear tensor analysis

NO magic!

New research directions

- Automatic mining
- Non-linear (gray-box) modeling
- Large-scale tensor analysis

Put all together

New challenge: MANT analysis

Multi-Aspect Non-linear Time-series

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[Matsubara+ KDD'14]

FUNNEL: Automatic Mining of Spatially Coevolving Epidemics

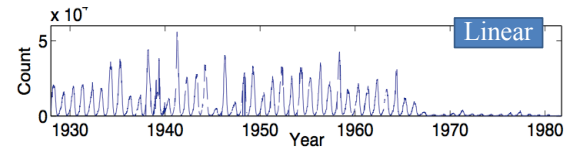
Yasuko Matsubara, Yasushi Sakurai (Kumamoto University)
 Willem G. van Panhuis (University of Pittsburgh)
 Christos Faloutsos (CMU)



http://www.cs.kumamoto-u.ac.jp/~yasuko/TALKS/17-KDD-tut/ © 2017 Sakurai, Matsubara & Faloutsos 67

Motivation

Given: Large set of epidemiological data
 e.g., Measles cases in the U.S.

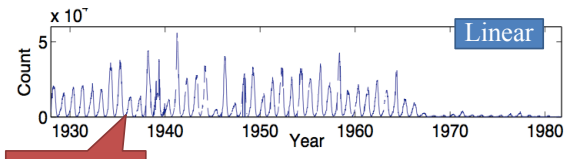


(Weekly)

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Motivation

Given: Large set of epidemiological data
 e.g., Measles cases in the U.S.

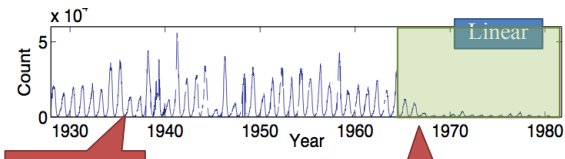


(Weekly)

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Motivation

Given: Large set of epidemiological data
 e.g., Measles cases in the U.S.

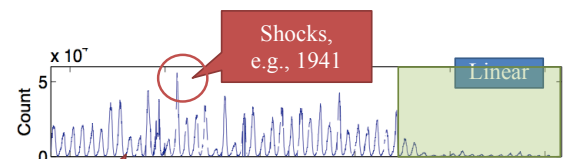


(Weekly)

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Motivation

Given: Large set of epidemiological data
 e.g., Measles cases in the U.S.



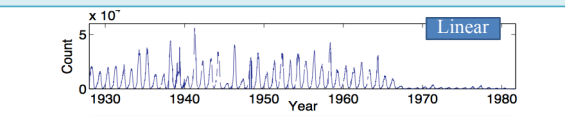
(Weekly)

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Motivation

Given: Large set of epidemiological data
 e.g., Measles cases in the U.S.

Goal: summarize all the epidemic time-series, **“fully-automatically”**



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Data description

Project Tycho: infectious diseases in the U.S.

56 diseases

50 states

1888 Time (weekly) (> 125 years)

PROJECT TYCHO DATA FOR HEALTH

\mathcal{X}

http://www.cs.kumamoto-u.ac.jp/~yasuko/TALKS/17-KDD-tut/ © 2017 Sakurai, Matsubara & Faloutsos 73

Data description

Project Tycho: infectious diseases in the U.S.

56 diseases

50 states

1888 Time (weekly) (> 125 years)

PROJECT TYCHO DATA FOR HEALTH

\mathcal{X}

x

Element x : # of cases
e.g., 'measles', 'NY', 'April 1-7, 1931', '4000'

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Problem definition

Given:
Tensor \mathcal{X} (disease x state x time)

\mathcal{X}

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Problem definition

Given:
Tensor \mathcal{X} (disease x state x time)

\mathcal{X}

Find:
Compact description of \mathcal{X} , "automatically"

\mathcal{X} = FUNNEL (B, R, N, E, M) (P1, P2, P3, P4, P5)

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Problem definition

Given:
Tensor \mathcal{X} (disease x state x time)

\mathcal{X}

Find:
Compact description of \mathcal{X} , "automatically"

Seasonality

Discontinuities

\mathcal{X} = FUNNEL (B, R, N, E, M) (P1, P2, P3, P4, P5)

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Problem definition

Given:
Tensor \mathcal{X} (disease x state x time)

\mathcal{X}

Find:
Compact description of \mathcal{X} , "automatically"

NO magic numbers!

Parameter-free!

\mathcal{X} = FUNNEL (B, R, N, E, M) (P1, P2, P3, P4, P5)

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Modeling power of FUNNEL

Our model can capture 5 properties

P1

Seasonality

P2

Disease reductions

P3

Area sensitivity

P4

External events

P5

Mistakes

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Modeling power of FUNNEL

P1

Seasonality

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Modeling power of FUNNEL

P1

Seasonality

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Modeling power of FUNNEL

P1

Seasonality

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Modeling power of FUNNEL

P1

Seasonality

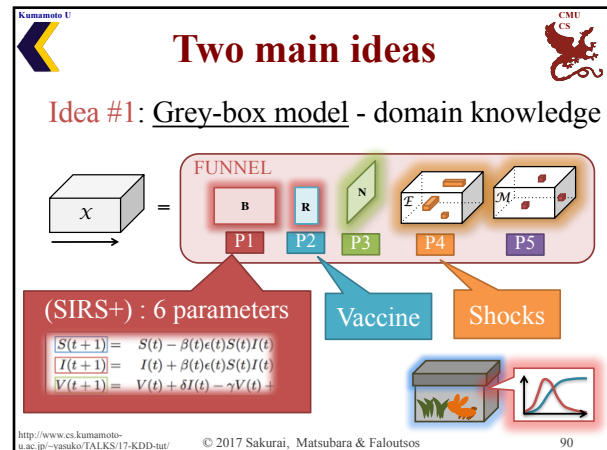
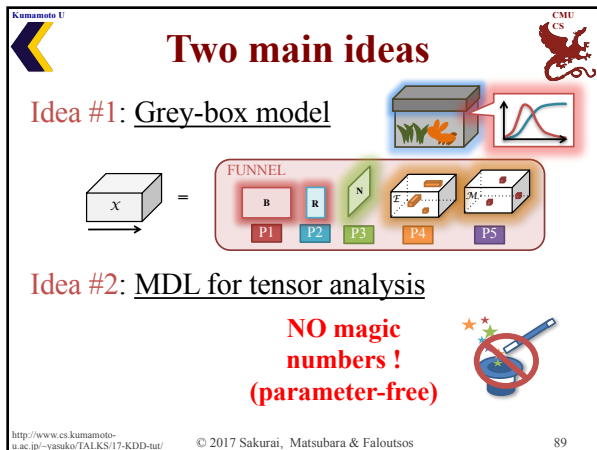
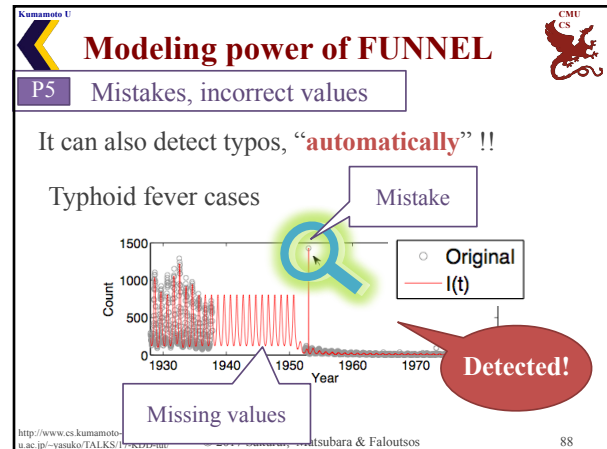
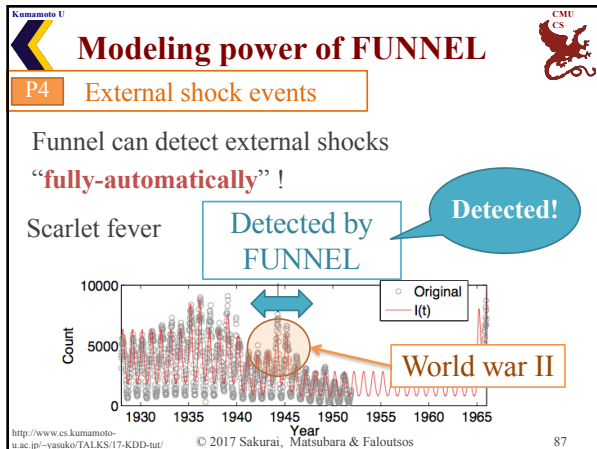
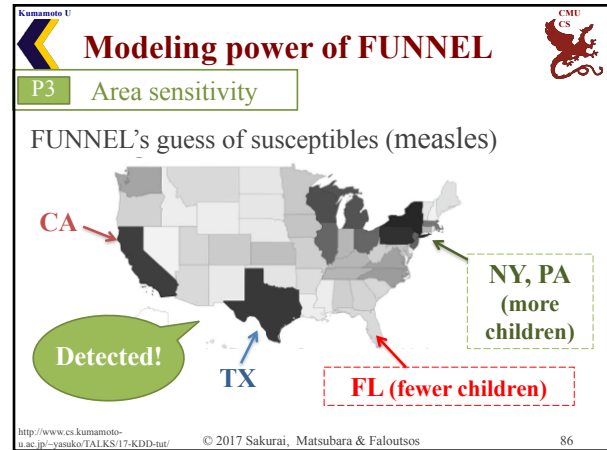
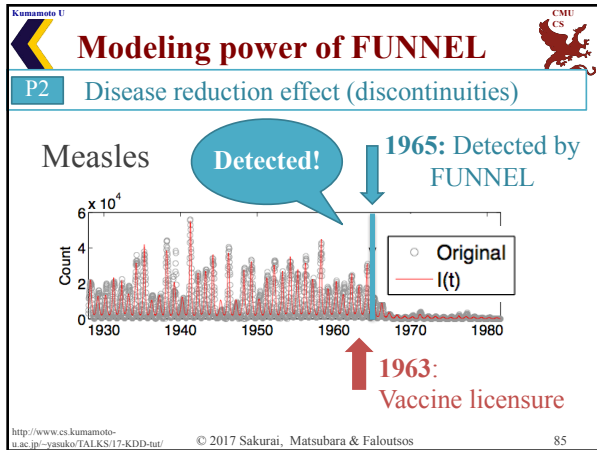
http://www.cs.kumamoto-u.ac.jp/~yasuko/TALKS/17-KDD-tut/ © 2017 Sakurai, Matsubara & Faloutsos 83

Modeling power of FUNNEL

P1

Seasonality

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Two main ideas

Idea #2: Fitting with MDL -> automatic!

Cost function

$$Cost_T(\mathcal{X}; \mathcal{F}) = \log^*(d) + \log^*(l) + \log^*(n) + Cost_M(\mathbf{B}) + Cost_M(\mathbf{R}) + Cost_M(\mathbf{N}) + Cost_M(\mathbf{E}) + Cost_M(\mathbf{M}) + Cost_C(\mathcal{X}|\mathcal{F})$$

NO magic numbers
Parameter-free!

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Proposed model: FUNNEL

(a) FUNNEL-single

(b) FUNNEL-full (tensor)

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Proposed model: FUNNEL

(a) FUNNEL-single

(b) FUNNEL-full (tensor)

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FUNNEL – with a single epidemic

Given: “single” epidemic sequence

e.g., measles in NY

Find: nonlinear equation, model parameters

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FUNNEL – with a single epidemic

With a single epidemic: Funnel-RE

People of 3 classes

- S : Susceptible
- I : Infected
- V : Vigilant/vaccinated

Details

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FUNNEL – with a single epidemic

With a single epidemic: Funnel-RE

$$\begin{aligned} S(t+1) &= S(t) - \beta(t)\epsilon(t)S(t)I(t) + \gamma V(t) - \theta(t)S(t) \\ I(t+1) &= I(t) + \beta(t)\epsilon(t)S(t)I(t) - \delta I(t) \\ V(t+1) &= V(t) + \delta I(t) - \gamma V(t) + \theta(t)S(t) \end{aligned} \quad (3)$$

S(t) : susceptible
I(t) : Infected
V(t) : Vigilant /Vaccinated

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FUNNEL – with a single epidemic

With a single epidemic: Funnel-RE

$$\begin{aligned} S(t+1) &= S(t) - \beta(t)\epsilon(t)S(t)I(t) + \gamma V(t) - \theta(t)S(t) \\ I(t+1) &= I(t) + \beta(t)\epsilon(t)S(t)I(t) - \delta I(t) \\ V(t+1) &= V(t) + \delta I(t) - \gamma V(t) + \theta(t)S(t) \end{aligned} \quad (3)$$

$\beta(t)$: strength of infection (yearly periodic func)

$$\beta(t) = \beta_0 \cdot \left(1 + P_a \cdot \cos\left(\frac{2\pi}{P_p}(t + P_s)\right)\right)$$

$$P_p = 52$$

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FUNNEL – with a single epidemic

With a single epidemic: Funnel-RE

$$\begin{aligned} S(t+1) &= S(t) - \beta(t)\epsilon(t)S(t)I(t) + \gamma V(t) - \theta(t)S(t) \\ I(t+1) &= I(t) + \beta(t)\epsilon(t)S(t)I(t) - \delta I(t) \\ V(t+1) &= V(t) + \delta I(t) - \gamma V(t) + \theta(t)S(t) \end{aligned} \quad (3)$$

δ : healing rate
 $\theta(t)$: disease reduction effect

$$\theta(t) = \begin{cases} 0 & (t < t_\theta) \\ \theta_0 & (t \geq t_\theta) \end{cases}$$

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FUNNEL – with a single epidemic

With a single epidemic: Funnel-RE

$$\begin{aligned} S(t+1) &= S(t) - \beta(t)\epsilon(t)S(t)I(t) + \gamma V(t) - \theta(t)S(t) \\ I(t+1) &= I(t) + \beta(t)\epsilon(t)S(t)I(t) - \delta I(t) \\ V(t+1) &= V(t) + \delta I(t) - \gamma V(t) + \theta(t)S(t) \end{aligned} \quad (3)$$

$\epsilon(t)$: temporal susceptible rate

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Proposed model: FUNNEL

single epidemic
Multi-evolving epidemics

(a) FUNNEL-single
(b) FUNNEL-full (tensor)

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FUNNEL-full

P1 P2 global/country P3 local/state

P4 P5 extra - \mathcal{E} : shocks & \mathcal{M} : mistakes

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FUNNEL-full

Global

P1 Base matrix \mathbf{B} ($d \times 6$)
P2 Disease reduction matrix \mathbf{R} ($d \times 2$)

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FUNNEL-full

Details

$X = N$

Local

P3 **Geo-disease matrix $N(d \times l)$**

$N = \{N_{ij}\}_{i,j=1}^{d,l}$: potential population of disease i in state j

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FUNNEL-full

Details

Extra

P4 **External shock tensor \mathcal{E}**

P5 **Mistake tensor \mathcal{M}**

P4 P5 extra - \mathcal{E} : shocks & \mathcal{M} : mistakes

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FUNNEL-full

Details

P4

$\mathcal{E} = \{E^{(D)}, E^{(T)}, E^{(S)}\}$

Disease matrix Time matrix State matrix

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Challenges

Q1. How to automatically

- find “external shocks” ?
- ignore “mistakes” (i.e., typos) ?

Q2. How to efficiently estimate model parameters ?

$X = \text{FUNNEL}(B, R, N, E, M)$

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Challenges

Q1. How to automatically

- find “external shocks” ?
- ignore “mistakes” (i.e., typos) ?

Idea (1): Model description cost

Q2. How to efficiently estimate model parameters ?

Idea (2): Multi-layer optimization - $O(dln)$

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FUNNEL at work - forecasting

Forecasting future epidemics

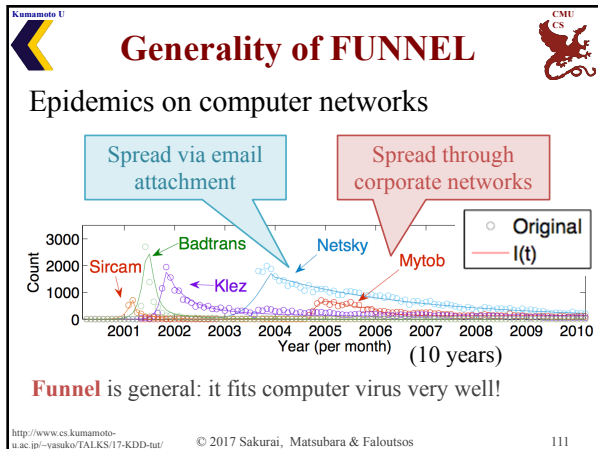
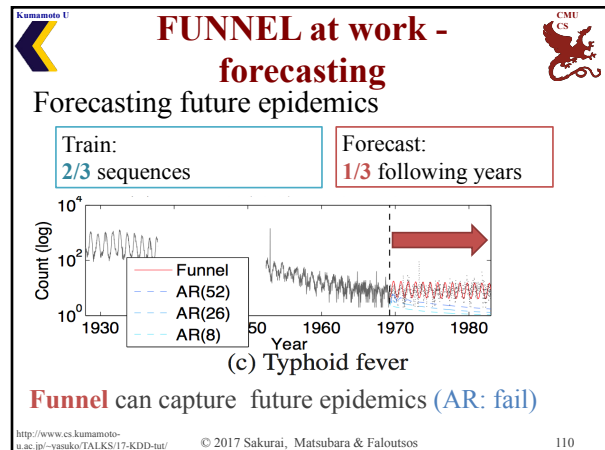
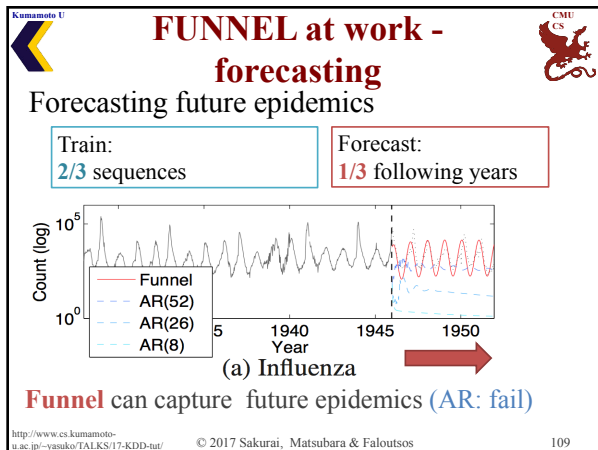
Train: 2/3 sequences Forecast: 1/3 following years

Count (log) vs Year

Legend: Funnel, AR(52), AR(26), AR(8)

(a) Influenza

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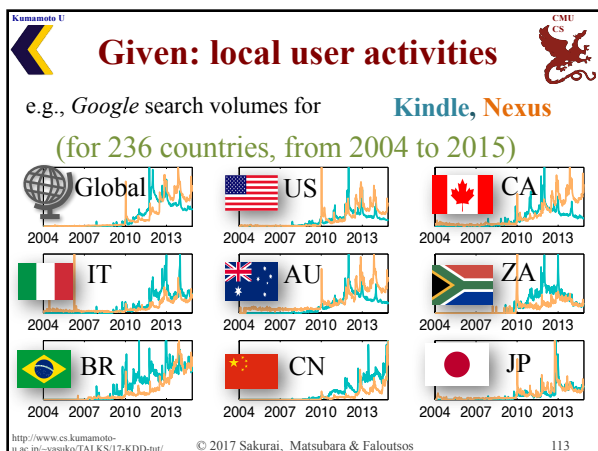


[Matsubara+ WWW'16]

Non-linear Mining of Competing Local Activities

Yasuko Matsubara (Kumamoto University)
 Yasushi Sakurai (Kumamoto University)
 Christos Faloutsos (CMU)

http://www.cs.kumamoto-u.ac.jp/~yasuko/TALKS/17-KDD-ut/ © 2017 Sakurai, Matsubara & Faloutsos 112





Data description

Time-stamped events: {activity, location, time}

Location m

Activity d

Time (weekly) n

\mathcal{X}

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Data description

Time-stamped events:

Location m

Activity d

Time n

\mathcal{X}

e.g., 'Kindle', 'US', 'April 1-7, 2014', '100'

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Problem definition

Given: Tensor \mathcal{X}
(activity \times location \times time)

Find: Compact description of \mathcal{X}

CompCube

B C S D

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Problem definition

Given: Tensor \mathcal{X}

Basics

Competition

Seasonality

Deltas

CompCube

B C S D

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Problem definition

Given: Tensor \mathcal{X}
(activity \times location \times time)

Global & Local

Find: Compact description of \mathcal{X}

CompCube

B C S D

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Problem definition

Given: Tensor \mathcal{X}
(activity \times location \times time)

Find: Compact description of \mathcal{X}

NO magic numbers!

Parameter-free!

B C S D

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Modeling power of CompCube

Products

News sources

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Modeling power of CompCube

Products

News sources

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Modeling power of CompCube

Q. Any global/local competition?

Nexus VS. Kindle

e.g., in

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Modeling power of CompCube

e.g., Google search volumes for **Kindle, Nexus**

Weak/Average/Strong

Local Competition strength

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Modeling power of CompCube

e.g., Google search volumes for **Kindle, Nexus**

Weak/Average/**Strong**

Local Competition strength

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Modeling power of CompCube

e.g., Google search volumes for **Kindle, Nexus**

Weak/Average/**Strong**

Local Competition strength

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Modeling power of CompCube

Products

News sources

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Modeling power of CompCube

Products

News sources

Q. Any seasonality?

in

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Modeling power of CompCube

e.g., Local seasonality for iPod

Component #1

Component #2

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Modeling power of CompCube

e.g., Local seasonality for iPod

Component #1

Component #2

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Modeling power of CompCube

e.g., Local seasonality for iPod

Component #1

Component #2

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Modeling power of CompCube

Products

News sources

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Modeling power of CompCube

Products

News sources

Q. Any world-wide events?

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Modeling power of CompCube

Fitting result for **News resources**

Fitting result – RMSE=0.056

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Modeling power of CompCube

Fitting result for **News resources**

Fitting result – RMSE

Detected!

US election Nov. 2008

Wikipedia

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Modeling power of CompCube

Fitting result for **News resources**

Fitting result – RMSE

Q. Which countries are interested in US politics?

Wikipedia

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Modeling power of CompCube

Fitting result for **News resources**

Weak/Strong

Local attention to US election

US election Nov. 2008

Wikipedia

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CompCube-dense

Given: x → Output: B, C, S, D


Basics

Competition

Seasonality

Deltas

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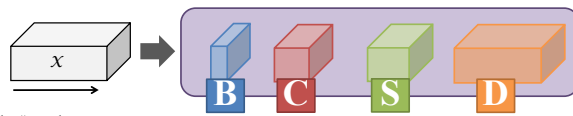
CompCube-dense  [Details](#)

Non-linear dynamical system


$$P_{il}(t) = P_{il}(t-1) \left[1 + r_{il} \left(1 - \frac{\sum_{j=1}^d c_{ijl} \cdot P_{jl}(t-1)}{K_{il}} \right) \right]$$

$$V_{il}(t) = P_{il}(t) [1 + s_{il}(t \bmod n_p)] + \delta_{il}(t)$$

$(i = 1, \dots, d; l = 1, \dots, m; t = 1, \dots, n) \quad P_{il}(0) = p_{il}$



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CompCube-dense  [Details](#)

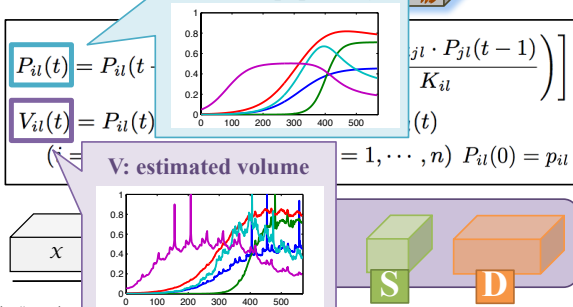
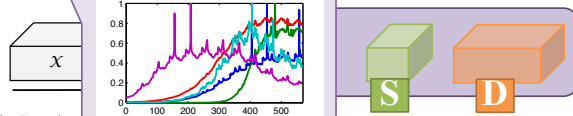
Non-linear **P: latent popularity**

$$P_{il}(t) = P_{il}(t-1) \left[1 + r_{il} \left(1 - \frac{\sum_{j=1}^d c_{ijl} \cdot P_{jl}(t-1)}{K_{il}} \right) \right]$$


$$V_{il}(t) = P_{il}(t) [1 + s_{il}(t \bmod n_p)] + \delta_{il}(t)$$

$(i = 1, \dots, d; l = 1, \dots, m; t = 1, \dots, n) \quad P_{il}(0) = p_{il}$

V: estimated volume

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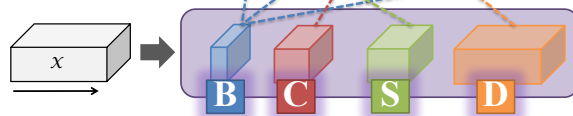
CompCube-dense  [Details](#)

Non-linear dynamical system


$$P_{il}(t) = P_{il}(t-1) \left[1 + r_{il} \left(1 - \frac{\sum_{j=1}^d c_{ijl} \cdot P_{jl}(t-1)}{K_{il}} \right) \right]$$

$$V_{il}(t) = P_{il}(t) [1 + s_{il}(t \bmod n_p)] + \delta_{il}(t)$$

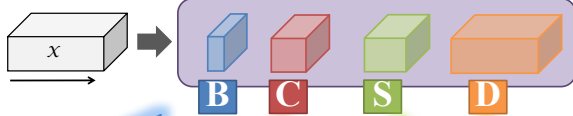
$(i = 1, \dots, d; l = 1, \dots, m; t = 1, \dots, n) \quad P_{il}(0) = p_{il}$



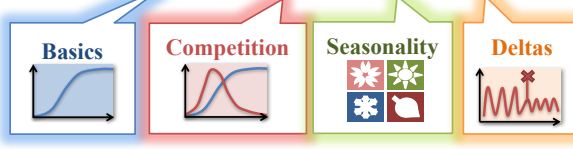
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Initial attempt: CompCube-dense 


Given: **CompCube-dense**




Basics **Competition** **Seasonality** **Deltas**



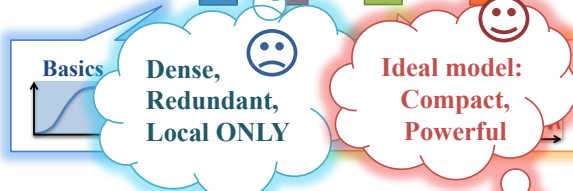
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Initial attempt: CompCube-dense 


Given: **CompCube-dense**



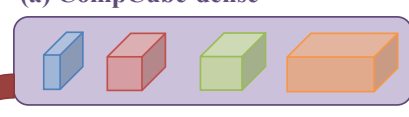
Basics **Dense, Redundant, Local ONLY** **Ideal model: Compact, Powerful**



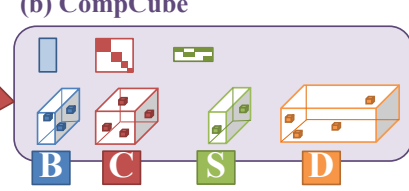
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Final model: CompCube 

(a) CompCube-dense



(b) CompCube



Compress & Summarize

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Final model: CompCube

(a) CompCube-dense

(b) CompCube

Global

B C S D

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Final model: CompCube

(a) CompCube-dense

(b) CompCube

Global

Local

B C S D

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Final model: CompCube

(a) CompCube-dense

Global

Local

B C S D

$C \approx C \cdot 2^{C'}$

Dense Sparse

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Algorithms

Q1. How can we efficiently estimate parameters?

Q2. How can we automatically find best parameter sets?

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Algorithms (Details in paper)

Q1. How can we efficiently estimate parameters?

Idea (1) : TetraFit algorithm

Q2. How can we automatically find best parameter sets?

Idea (2) : Model description cost

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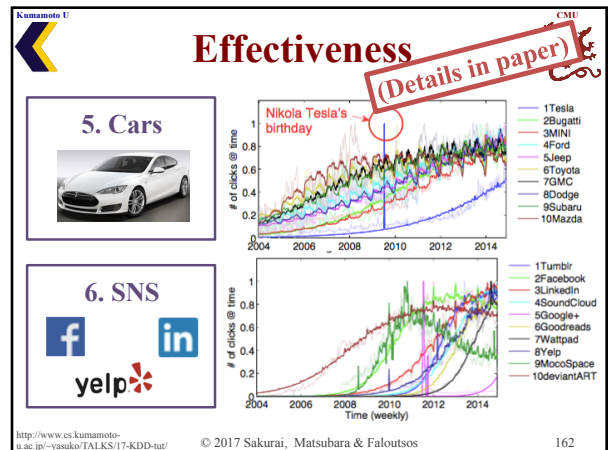
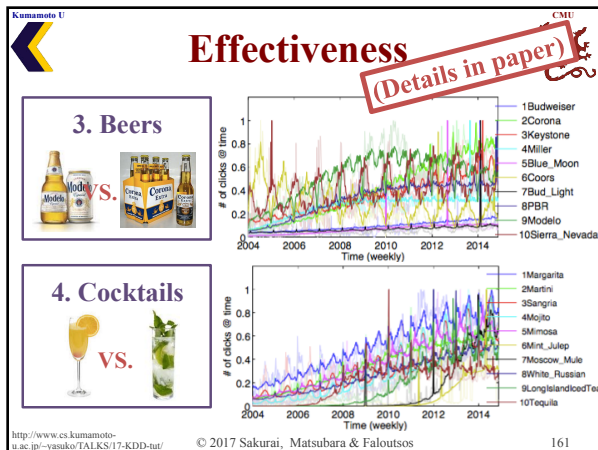
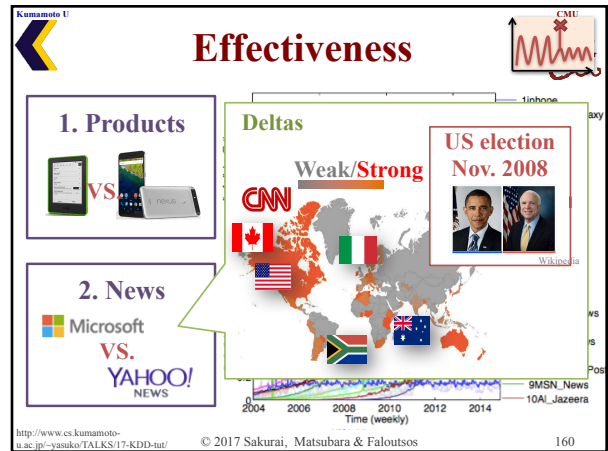
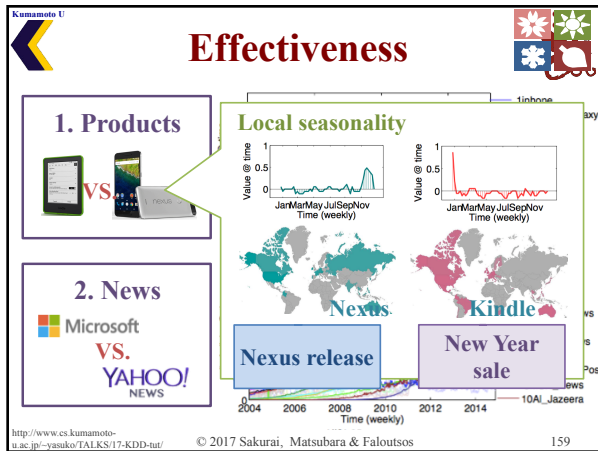
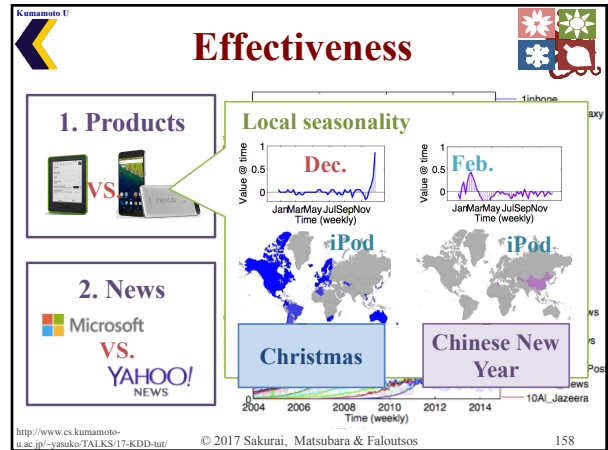
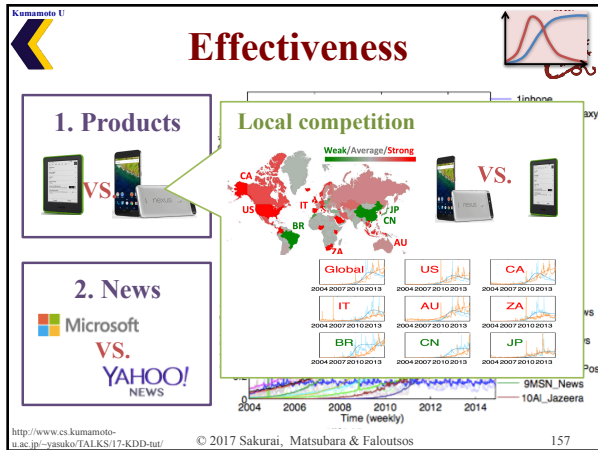
Effectiveness

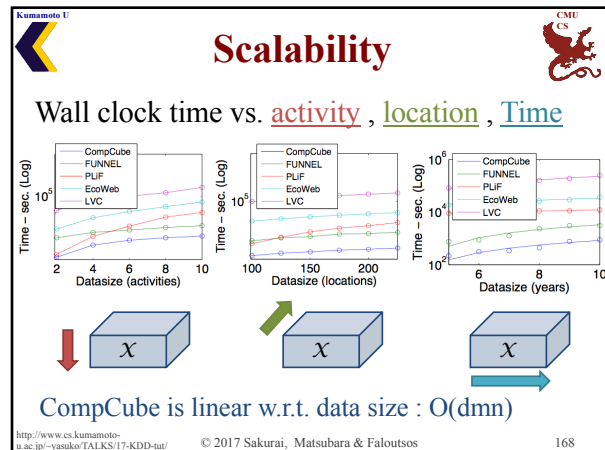
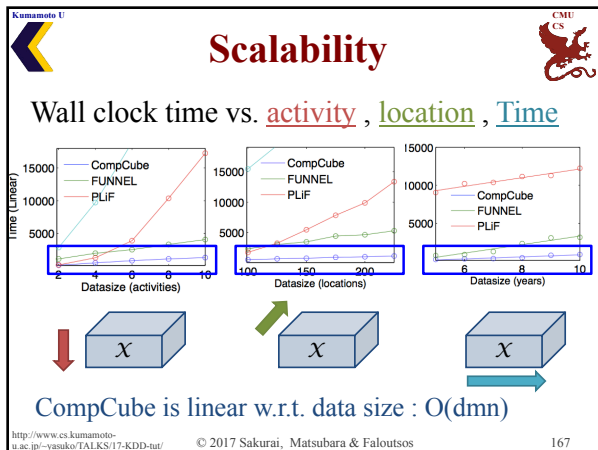
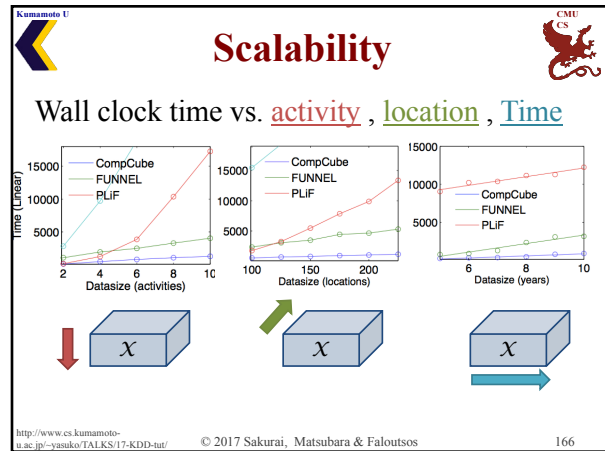
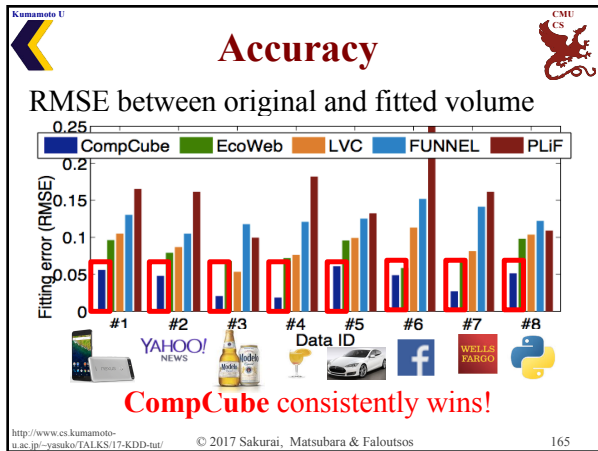
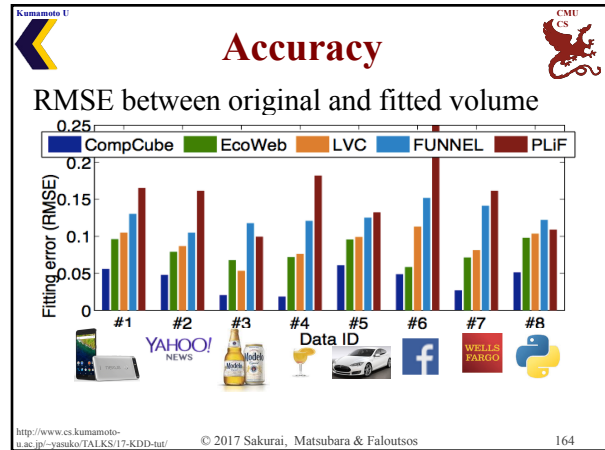
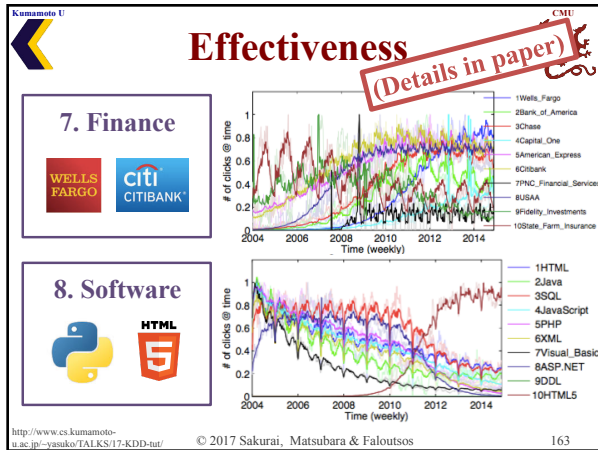
1. Products

2. News

US election

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CompCube at work - forecasting

Forecasting future local activities

Location:

Activity:

Time (weekly):

Train: 2/3 sequences Forecast: 1/3 following years

X

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CompCube at work - forecasting

Forecasting results for #1 Products

1. Products

Original sequence

CompCube (RMSE=0.2600)

SARIMA+ (RMSE=0.4369)

TBATS (RMSE=0.5839)

CompCube captures future activities very well

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CompCube at work - forecasting

Forecasting error (original vs. forecasts)

Forecasting error

Data ID: #1, #2, #3, #4, #5, #6, #7, #8

YAHOO! NEWS,

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CompCube at work - forecasting

Forecasting error (original vs. forecasts)

Forecasting error

Data ID: #1, #2, #3, #4, #5, #6, #7, #8

YAHOO! NEWS,

CompCube consistently wins!

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Part 3 Conclusions

- Real data are often in high dimensions with multiple aspects (modes)
- Matrices and tensors provide elegant theory and algorithms
- MANT analysis

Multi-Aspect Non-linear Time-series

$X \approx \dots + \dots$

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Part 3



Extension of time-series: tensor analysis

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Yasuko Matsubara (Kumamoto University)

Christos Faloutsos (Carnegie Mellon University)

<http://www.cs.kumamoto-u.ac.jp/~yasuko/TALKS/17-KDD-tut/>

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