



Smart Analytics for Big Time-series Data


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Roadmap

- Motivation
- **Similarity search, pattern discovery and summarization** Part 1
- Non-linear modeling and forecasting Part 2
- Extension of time-series data: tensor analysis Part 3



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Part 1

Similarity search, pattern discovery and summarization

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Part 1 - Roadmap

- ➔ Motivation
 - Similarity Search and Indexing
 - Feature extraction
 - Linear forecasting
 - Streaming pattern discovery
 - Automatic mining



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Motivation - Applications

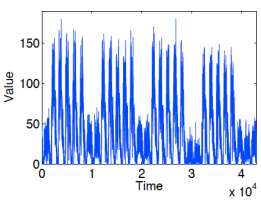
- Web online activities
 - Web access logs
 - Search volume
 - Online reviews
- IoT device data
- Medical, healthcare data

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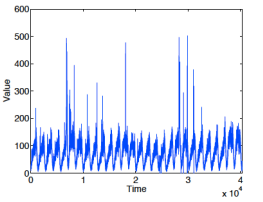



Motivation - Applications

- Web access logs



Web clicks (business news site)



Ondemand TV (access count of users)

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Motivation - Applications

- Web search volume from Google trends

Compare Search terms: Internet of Things

Interest over time

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Motivation - Applications

- IoT (Internet of Things) device data
 - Civil/automobile infrastructure
 - Bridge vibrations [Oppenheim+02]
 - Road conditions / traffic monitoring
 - Environmental data (air/water pollutant monitoring)

Automobile traffic

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Motivation - Applications

- Medical (epidemic) time-series data e.g., measles cases in the U.S.

Count $\times 10^7$

Yearly periodicity

Shocks, e.g., 1941

Vaccine effect

Year (Weekly)

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Wish list

- Problem 1: find patterns/rules
- Problem 2: forecast
- Problem 3: find patterns/rules/forecast, with many time sequences

Number of packets sent

1 3 5 7 9 11

1 3 5 7 9 11

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Problem #1

Given: time-series data (e.g., #clicks over time)
Find: patterns, periodicities, and/or compress

Original web-click sequence

Weekday component

Weekend component

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Problem #2

Given x_t, x_{t-1}, \dots , forecast x_{t+1}

Number of packets sent

Time Tick

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Problem #3

- Given: A set of **correlated** time sequences
- Forecast **'Repeated(t)'**

Number of packets

Time Tick

Legend: sent (red), lost (blue), repeated (green)

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Important observations

Patterns, outliers, modeling, forecasting and similarity indexing are closely related:

- For forecasting, we need
 - patterns/rules/models
 - similar past settings
- For outliers, we need to have forecasts
 - (outlier = too far away from our forecast)

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Important topics NOT in this tutorial:

- Continuous queries
 - [Babu+Widom] [Gehrke+] [Madden+]
- Categorical data streams
 - [Hatonen+96]
- Outlier detection (discontinuities)
 - [Breunig+00]

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Roadmap

- Motivation
- Similarity Search and Indexing
- Feature extraction
- Linear forecasting
- Streaming pattern discovery
- Automatic mining

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Roadmap

- Motivation
- Similarity Search and Indexing
 - distance functions: Euclidean, time-warping
 - indexing
- Feature extraction
- Linear forecasting
- Streaming pattern discovery
- Automatic mining

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Importance of distance functions

Subtle, but **absolutely necessary**:

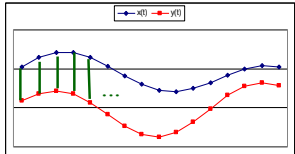
- A 'must' for similarity search, indexing and clustering

Two major families

- Euclidean and Lp norms
- Time warping and variations

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Euclidean and Lp



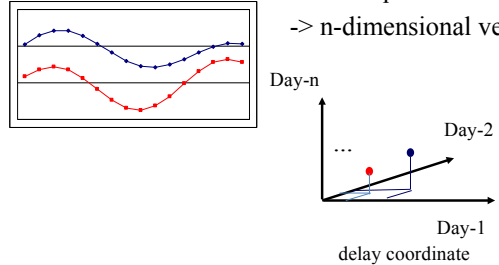
$$D(\bar{x}, \bar{y}) = \sum_{i=1}^n (x_i - y_i)^2$$

$$L_p(\bar{x}, \bar{y}) = \sum_{i=1}^n |x_i - y_i|^p$$

- L_1 : city-block = Manhattan
- L_2 = Euclidean
- L_∞

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Observation #1

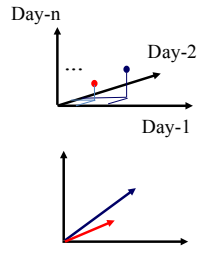


- Time sequence
-> n-dimensional vector

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Observation #2

- Euclidean distance is closely related to
 - cosine similarity
 - dot product
 - 'cross-correlation' function



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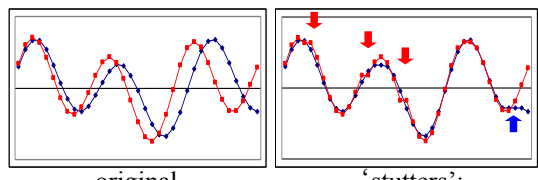
Time Warping

- allow accelerations - decelerations
- (with or w/o penalty)
- THEN compute the (Euclidean) distance (+ penalty)
- related to the string-editing distance
- fast search methods [Yi+98] [Keogh+02] [Sakurai+05]

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Time Warping

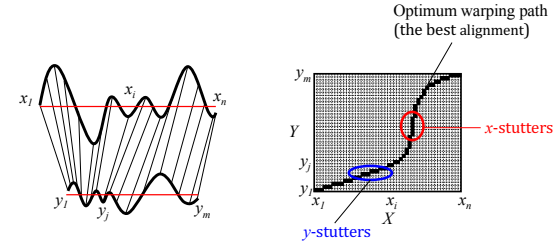
- Allow sequences to be stretched along the time axis
 1. minimize the distance of sequences
 2. insert 'stutters' into a sequence
 3. THEN compute the (Euclidean) distance



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Time Warping

Q: how to compute it?
A: dynamic programming



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Time Warping DETAILS

Q: how to compute it?
 A: dynamic programming

$$X = \{x_1, x_2, \dots, x_i\}, Y = \{y_1, y_2, \dots, y_j\}$$

$$D_{d_{tw}}(X, Y) = f(n, m)$$

$$f(i, j) = \|x_i - y_j\| + \min \begin{cases} f(i, j-1) & \text{x-stutter} \\ f(i-1, j) & \text{y-stutter} \\ f(i-1, j-1) & \text{no stutter} \end{cases}$$

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Time Warping

- Time warping matrix & optimal path:

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Time Warping

- Time warping matrix & optimal path:

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Time Warping - variations

- Time warping matrix & optimal path:

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Time Warping - variations

- Time warping matrix & optimal path:

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Time warping

- Complexity: $O(M*N)$ - quadratic on the length of the strings
- Many** variations (penalty for stutters; limit on the number/percentage of stutters; ...)
- popular in voice processing [Rabiner+Juang]

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A variation: Uniform axis scaling

- Stretch / shrink time axis of Y, up to p%, for free
- THEN compute Euclidean distance
- [Keogh+, VLDB04]

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Other Distance functions

- piece-wise linear/flat approx.; compare pieces [Keogh+01] [Faloutsos+97]
- ‘cepstrum’ (for voice [Rabiner+Juang])
 - do DFT; take log of amplitude; do DFT again!
- Allow for small gaps [Agrawal+95]

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Related work

- Chen + Ng [vldb’ 04]: ERP ‘Edit distance with Real Penalty’: give a penalty to stutters
- Keogh+ [kdd’ 04]: VERY NICE, based on information theory: compress each sequence (quantize + Lempel-Ziv), using the **other** sequences’ LZ tables
- Rakthanmanon+ [kdd’ 12]: EXCELLENT Software, the UCR Suite for ultrafast subsequence search

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Conclusions

- Prevailing distances:
 - Euclidean and
 - time-warping

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Roadmap

- Motivation
- Similarity Search and Indexing
 - distance functions: Euclidean, time-warping
 - ➔ – indexing
- Feature extraction
- Linear forecasting
- Streaming pattern discovery
- Automatic mining

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Indexing

- Given a set of time sequences,
- Find the ones similar to a desirable query sequence

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Indexing

Price

1 365 day

Price

1 365 day

Price

1 365 day

distance function: by expert
(Euclidean; DTW; ...)

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Idea: 'GEMINI'

Eg., 'find stocks similar to MSFT'

Seq. scanning: too slow

How to accelerate the search?

[Faloutsos96]

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'GEMINI' - Pictorially

S1

1 365 day

Sn

1 365 day

eg., std

• F(S1)

feature vectors

• F(Sn)

eg, avg

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GEMINI

Solution: Quick-and-dirty' filter:

- extract d features (numbers, eg., avg., etc.)
- map into a point in the d -dimensional feature space
- organize points with off-the-shelf spatial access method ('SAM' – R-tree, etc)
- discard false alarms

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Examples of GEMINI

- Time sequences: DFT (up to 100 times faster) [SIGMOD94];
- [Kanellakis+], [Mendelzon+]

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Indexing - SAMs

Q: How do Spatial Access Methods (SAMs) work?

A: they group nearby points (or regions) together, on nearby disk pages, and answer spatial queries quickly ('range queries', 'nearest neighbor' queries etc)

For example:

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R-trees

- [Guttman84] eg., w/ fanout 4: group nearby rectangles to parent MBRs; each group -> disk page

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R-trees

- eg., w/ fanout 4:

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R-trees

- eg., w/ fanout 4:

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R-trees - range search?

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R-trees - range search?

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Conclusions

- Fast indexing: through GEMINI
 - feature extraction and
 - (off the shelf) Spatial Access Methods [Gaede+98]

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Roadmap

- Motivation
- Similarity Search and Indexing
- ➔ • Feature extraction
- Linear forecasting
- Streaming pattern discovery
- Automatic mining

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Roadmap

- Motivation
- Similarity Search and Indexing
- Feature extraction
 - ➔ – DFT, DWT (data independent)
 - SVD, ICA (data independent)
 - MDS, FastMap
- Linear forecasting
- Streaming pattern discovery
- Automatic mining

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DFT: definition

- For a sequence x_0, x_1, \dots, x_{n-1}
- the (**n-point**) Discrete Fourier Transform is
- X_0, X_1, \dots, X_{n-1} :

$$X_f = 1/\sqrt{n} \sum_{t=0}^{n-1} x_t * \exp(-j2\pi tf/n) \quad f = 0, \dots, n-1$$

$$(j = \sqrt{-1})$$

$$x_t = 1/\sqrt{n} \sum_{f=0}^{n-1} X_f * \exp(+j2\pi tf/n) \quad \swarrow \text{inverse DFT}$$

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DFT: Amplitude spectrum

Amplitude: $A_f^2 = \text{Re}^2(X_f) + \text{Im}^2(X_f)$

count

year

Ampl.

Freq.

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DFT: examples

- Flat

Amplitude

time

freq

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DFT: examples

- Low frequency sinusoid

time

freq

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DFT: examples

- Sinusoid - symmetry property: $X_f = X_{n-f}^*$

time freq

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DFT: examples

- Higher freq. sinusoid

time freq

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DFT: examples

- Examples

time freq

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DFT: examples

- Examples

time freq

Ampl.
Freq.

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DFT: Amplitude spectrum

Amplitude: $A_f^2 = \text{Re}^2(X_f) + \text{Im}^2(X_f)$

count

year

Ampl.
Freq.

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DFT: Amplitude spectrum

count

year

Ampl.
Freq.

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DFT: Amplitude spectrum

count

year

Ampl.

freq=0

freq=12

Freq.

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DFT: Amplitude spectrum

- Excellent approximation, with only 2 frequencies!
- So what?

Freq.

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DFT: Amplitude spectrum

- Excellent approximation, with only 2 frequencies!
- So what?
- A1: (lossy) compression
- A2: pattern discovery

Freq.

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DFT: Amplitude spectrum

- Excellent approximation, with only 2 frequencies!
- So what?
- A1: (lossy) compression
- A2: **pattern discovery**

Freq.

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Wavelets - DWT

- DFT is great - but, how about compressing a spike?

value

time

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Wavelets - DWT

- DFT is great - but, how about compressing a spike?
- A: Terrible - all DFT coefficients needed!

value

time

Ampl.

Freq.

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Wavelets - DWT

- DFT is great - but, how about compressing a spike?
- A: Terrible - all DFT coefficients needed!

value

time

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Wavelets - DWT

- Similarly, DFT suffers on short-duration waves (eg., baritone, silence, soprano)

value

time

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Wavelets - DWT

- Solution#1: Short window Fourier transform (SWFT)
- But: how short should be the window?

freq

time

value

time

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Wavelets - DWT

- Answer: **multiple** window sizes! -> DWT
- **'Multi-scale windows'**: brilliant idea that we'll see several times in this tutorial (BRAID, TriMine, etc)

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Wavelets - DWT

- Answer: **multiple** window sizes! -> DWT

Time domain

Multi-scale windows

	DFT	SWFT	DWT
freq			
time			

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Haar Wavelets

- subtract sum of left half from right half
- repeat recursively for quarters, eighthths, ...

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Wavelets - construc DETAILS

$x_0 \ x_1 \ x_2 \ x_3 \ x_4 \ x_5 \ x_6 \ x_7$

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Wavelets - construc DETAILS

level 1 $d_{1,0}$ $s_{1,0}$ $d_{1,1}$ $s_{1,1}$

$x_0 \ x_1 \ x_2 \ x_3 \ x_4 \ x_5 \ x_6 \ x_7$

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Wavelets - construc DETAILS

level 2 $d_{2,0}$ $s_{2,0}$

$d_{1,0}$ $s_{1,0}$ $d_{1,1}$ $s_{1,1}$

$x_0 \ x_1 \ x_2 \ x_3 \ x_4 \ x_5 \ x_6 \ x_7$

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Wavelets - construc DETAILS

etc ...

$d_{2,0}$ $s_{2,0}$

$d_{1,0}$ $s_{1,0}$ $d_{1,1}$ $s_{1,1}$

$x_0 \ x_1 \ x_2 \ x_3 \ x_4 \ x_5 \ x_6 \ x_7$

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Wavelets - construc DETAILS

Q: map each coefficient on the time-freq. plane

f

t

$d_{2,0}$ $s_{2,0}$

$d_{1,0}$ $s_{1,0}$ $d_{1,1}$ $s_{1,1}$

$x_0 \ x_1 \ x_2 \ x_3 \ x_4 \ x_5 \ x_6 \ x_7$

http://www.es.kumamoto-u.ac.jp/~yasuko/TALKS/17-KDD-tut/ © 2017 Sakurai, Matsubara & Faloutsos 77

Wavelets - construc DETAILS

Q: map each coefficient on the time-freq. plane

f

t

$d_{2,0}$ $s_{2,0}$

$d_{1,0}$ $s_{1,0}$ $d_{1,1}$ $s_{1,1}$

$x_0 \ x_1 \ x_2 \ x_3 \ x_4 \ x_5 \ x_6 \ x_7$

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Wavelets - construc DETAILS

Observation1:
 '+' can be some weighted addition
 '-' is the corresponding weighted difference ('Quadrature mirror filters')

Observation2: unlike DFT/DCT, there are *many* wavelet bases: Haar, Daubechies-4, Daubechies-6, Coifman, Morlet, Gabor, ...

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Wavelets - how do they look like?

- E.g., Daubechies-4

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Wavelets - how do they look like?

- E.g., Daubechies-4

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Wavelets - Drill#1:

- Q: baritone/silence/soprano - DWT?

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Wavelets - Drill#1:

- Q: baritone/silence/soprano - DWT?

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Wavelets - Drill#2:

- Q: spike - DWT?

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Wavelets - Drill#2:

- Q: spike - DWT?

0.00 0.00 0.71 0.00
0.00 0.50
-0.35
0.35

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Wavelets - Drill#3:

- Q: weekly + daily periodicity, + spike - DWT?

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Wavelets - Drill#3:

- Q: **weekly** + daily periodicity, + spike - DWT?

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Wavelets - Drill#3:

- Q: weekly + **daily** periodicity, + spike - DWT?

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Wavelets - Drill#3:

- Q: weekly + daily periodicity, + **spike** - DWT?

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Wavelets - Drill#3:

- Q: weekly + daily periodicity, + spike - DWT?

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Wavelets - Drill#3:

- Q: DFT?

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Advantages of Wavelets

- Better compression (better RMSE with same number of coefficients - used in JPEG-2000)
- fast to compute (usually: $O(n)$!)
- very good for 'spikes'

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DFT & DWT: conclusions

- DFT** spots periodicities (with the 'amplitude spectrum')
 - can be quickly computed ($O(n \log n)$), thanks to the FFT algorithm.
 - **standard** tool in signal processing (speech, image etc signals)
 - (closely related to DCT and JPEG)

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DFT & DWT: conclusions

- DWT**: multi-resolution
 - very suitable for self-similar traffic
 - used for summarization of streams [Gilbert+01], db histograms, etc
- DFT&DWT**: powerful tools for **compression, pattern detection** in real signals
 - included in math packages (matlab, 'R', mathematica, ... - often in spreadsheets!)

http://www.es.kumamoto-u.ac.jp/~yasuko/TALKS/17-KDD-tut/ © 2017 Sakurai, Matsubara & Faloutsos 94

Resources - software and urls

- <http://www.dsptutor.freeuk.com/jsanalyser/FTSpectrumAnalyser.html> : Nice java applets for FFT
- <http://www.relisoft.com/freeware/freq.html> voice frequency analyzer (needs microphone)

http://www.es.kumamoto-u.ac.jp/~yasuko/TALKS/17-KDD-tut/ © 2017 Sakurai, Matsubara & Faloutsos 95

Resources: software and urls

- xwpl*: open source wavelet package from Yale, with excellent GUI
- <http://monet.me.ic.ac.uk/people/gavin/java/waveletDemos.html> : wavelets and scalograms

http://www.es.kumamoto-u.ac.jp/~yasuko/TALKS/17-KDD-tut/ © 2017 Sakurai, Matsubara & Faloutsos 96

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Books

- William H. Press, Saul A. Teukolsky, William T. Vetterling and Brian P. Flannery: *Numerical Recipes in C*, Cambridge University Press, 1992, 2nd Edition. (Great description, intuition and code for DFT, DWT)
- C. Faloutsos: *Searching Multimedia Databases by Content*, Kluwer Academic Press, 1996 (introduction to DFT, DWT)

http://www.cs.kumamoto-u.ac.jp/~yasuko/TALKS/17-KDD-tut/ © 2017 Sakurai, Matsubara & Faloutsos 97

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Additional Reading

- [Gilbert+01] Anna C. Gilbert, Yannis Kotidis and S. Muthukrishnan and Martin Strauss, *Surfing Wavelets on Streams: One-Pass Summaries for Approximate Aggregate Queries*, VLDB 2001

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Roadmap

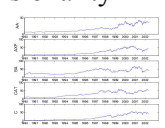
- Motivation
- Similarity Search and Indexing
- Feature extraction
 - DFT, DWT, DCT (data independent)
 - ➔ – SVD, ICA (data independent)
 - MDS, FastMap
- Linear forecasting
- Streaming pattern discovery
- Automatic mining

http://www.cs.kumamoto-u.ac.jp/~yasuko/TALKS/17-KDD-tut/ © 2017 Sakurai, Matsubara & Faloutsos 99

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SVD

- Singular Value Decomposition
- THE optimal method for dimensionality reduction
 - (under the Euclidean metric)
- Given: many time sequences
- Find: the latent ('hidden') variables



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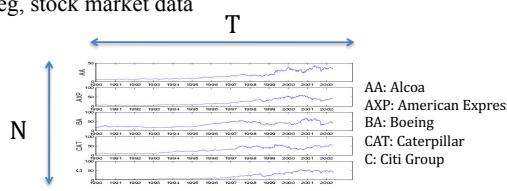
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SVD

Two (equivalent) interpretations:

- Geometric (each sequence -> point in T-d space)
- Matrix algebra ($N \times T$ matrix)

eg, stock market data



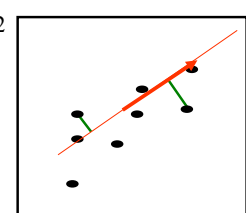
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Singular Value Decomposition (SVD)

- SVD (~LSI ~ KL ~ PCA ~ spectral analysis...) – Geometric interpretation

day2



day1

LSI: S. Dumais; M. Berry
 KL: eg, Duda+Hart
 PCA: eg., Jolliffe
 Details: [Press+], [Faloutsos96]

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SVD – matrix interpretation

- SVD -> matrix factorization: finds blocks

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SVD

- Extremely** useful tool
 - (also behind PageRank/google and Kleinberg's algorithm for hubs and authorities)

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SVD

- Extremely** useful tool
 - (also behind PageRank/google and Kleinberg's algorithm for hubs and authorities)
- But may be slow: $O(N * M * M)$ if $N > M$
- any approximate, faster method?

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SVD shortcuts

- random projections (Johnson-Lindenstrauss thm [Papadimitriou+ pods98])

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Random projections

- pick 'enough' random directions (will be ~orthogonal, in high-d!!)
- distances are preserved probabilistically, within epsilon
- (also, use as a pre-processing step for SVD [Papadimitriou+ PODS98])

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SVD & improvement

- Q: Can we do even better?
- A: sometimes, yes – by shooting for sparsity

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Independent Component Analysis (ICA)

- PCA (or SVD) sometimes misses essential features
 - PCA vs. ICA

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A.k.a.: BSS = cocktail party problem

Find hidden variables

- Untangle two sound sources

= "blind source separation"

- unknown sources,
- unknown mixing

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ICA

- Why not PCA

Source: Source #1, Source #2, Source #3
 Mix: Sequence #1 (Sources #1 & #3), Sequence #2 (Sources #2 & #3), Sequence #3 (Mix of all 3 sources)

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ICA

- Why not PCA

Source: Source #1, Source #2, Source #3
 Mix: Sequence #1 (Sources #1 & #3), Sequence #2 (Sources #2 & #3), Sequence #3 (Mix of all 3 sources)

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ICA

- Why not PCA

PCA: PC1, PC2, PC3
 ICA: IC1, IC2, IC3

ICA recognizes the components successfully and separately

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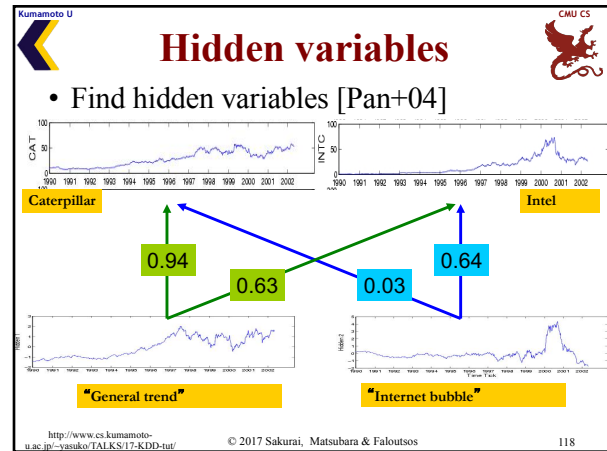
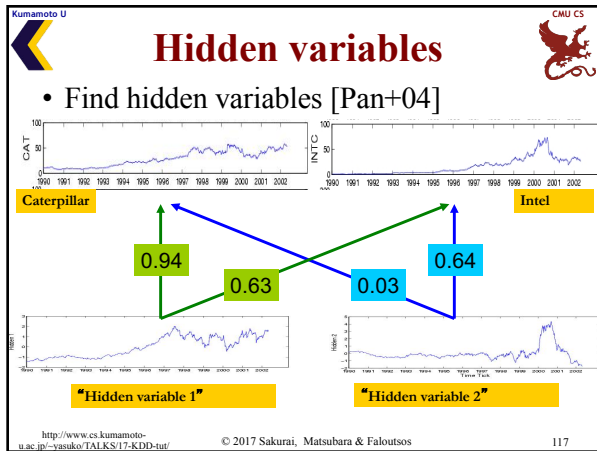
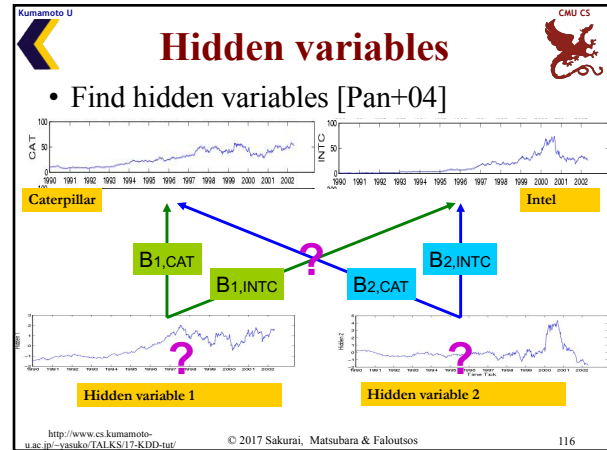
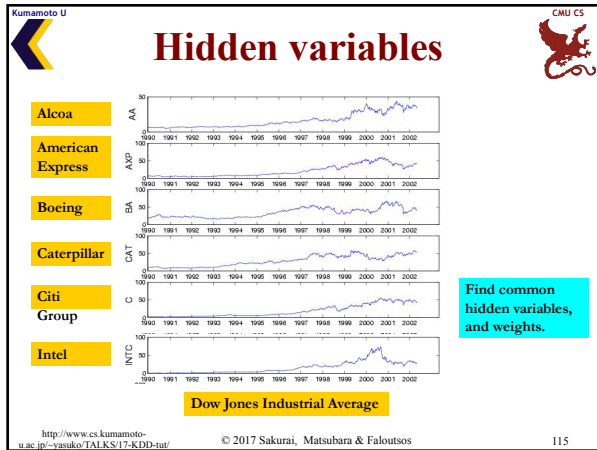
Hidden variables

- Local component analysis [Sakurai+11]

Original sequence: Anomaly spikes
 Weekly pattern, Daily pattern
 (b) Weekly pattern (WindMine), (c) Daily pattern (WindMine)
 (d) Weekly pattern (PCA), (e) Daily pattern (PCA)

PCA: failed

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Motivation: Find hidden variables

- ICA: also known as ‘Blind Source Separation’
- ‘cocktail party problem’
 - in a party, we can hear two concurrent conversations,
 - but separate them (and tune-in on one of them only)
- http://www.cnl.salk.edu/~tewon/Blind/blind_audio.html
- (in stocks: one ‘discussion’ is the general economy trend; the other ‘discussion’ is the tech-stock boom)

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Citation

- AutoSplit: Fast and Scalable Discovery of Hidden Variables in Stream and Multimedia Databases*, Jia-Yu Pan, Hiroyuki Kitagawa, Christos Faloutsos and Masafumi Hamamoto, PAKDD 2004, Sydney, Australia.
- WindMine: Fast and Effective Mining of Web-click Sequences*, Yasushi Sakurai, Lei Li, Yasuko Matsubara, Christos Faloutsos, SDM 2011, Mesa, Arizona.

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Roadmap

- Motivation
- Similarity Search and Indexing
- Feature extraction
 - DFT, DWT, DCT (data independent)
 - SVD, ICA (data independent)
 - ➔ – MDS, FastMap
- Linear forecasting
- Streaming pattern discovery
- Automatic mining

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MDS / FastMap

- but, what if we have NO points to start with? (eg. Time-warping distance)
- A: Multi-dimensional Scaling (MDS) ; FastMap

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MDS/FastMap

	O1	O2	O3	O4	O5
O1	0	1	1	100	100
O2	1	0	1	100	100
O3	1	1	0	100	100
O4	100	100	100	0	1
O5	100	100	100	1	0

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MDS

Multi Dimensional Scaling

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FastMap

- Multi-dimensional scaling (MDS) can do that, but in $O(N^2)$ time
- FastMap [Faloutsos+95] takes $O(N)$ time

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FastMap: Application

VideoTrails [Kobla+97]


scene-cut detection (about 10% errors)

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Variations

- Isomap [Tenenbaum, de Silva, Langford, 2000]
- LLE (Local Linear Embedding) [Roweis, Saul, 2000]
- MVE (Minimum Volume Embedding) [Shaw & Jebara, 2007]



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Conclusions - Practitioner's guide

Similarity search in time sequences

- 1) establish/choose distance (Euclidean, time-warping,...)
- 2) extract features (SVD, ICA, DWT), and use an SAM (R-tree/variant, or a Metric Tree M-tree)
- 2') for high intrinsic dimensionalities, consider sequential scan (it might win...)

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Books

- William H. Press, Saul A. Teukolsky, William T. Vetterling and Brian P. Flannery: *Numerical Recipes in C*, Cambridge University Press, 1992, 2nd Edition. (Great description, intuition and code for SVD)
- C. Faloutsos: *Searching Multimedia Databases by Content*, Kluwer Academic Press, 1996 (introduction to SVD, and GEMINI)

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- Eamonn J. Keogh, [Themis Palpanas](#), [Victor B. Zordan](#), [Dimitrios Gunopulos](#), [Marc Cardle](#): Indexing Large Human-Motion Databases. [VLDB 2004](#): 780-791


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Roadmap

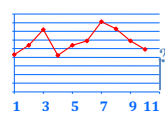
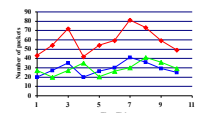
- Motivation
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Wish list

- Problem 1: find patterns/rules
- ➡ Problem 2: **forecast**
- Problem 3: find patterns/rules/forecast, with **many** time sequences

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Forecasting

"Prediction is very difficult, especially about the future." - Niels Bohr

<http://www.hfac.uh.edu/MediaFutures/thoughts.html>



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Roadmap

- Motivation
- Similarity Search and Indexing
- Feature extraction
- Linear forecasting
 - ➡ – Auto-regression: Least Squares; RLS
 - Co-evolving time sequences
- Streaming pattern discovery
- Automatic mining

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Problem: Forecasting

- Example: give x_{t-1}, x_{t-2}, \dots , forecast x_t

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Forecasting: Preprocessing

MANUALLY:
remove trends
periodicities

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Problem: Forecast

- Solution: try to express x_t as a linear function of the past: x_{t-2}, x_{t-3}, \dots (up to a window of w)

Formally:

$$x_t \approx a_1 x_{t-1} + \dots + a_w x_{t-w} + noise$$

(if we **know** it is a non-linear model, see Part 2)

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(Problem: Back-cast; interpolate)

- Solution - interpolate: try to express x_t as a linear function of the past AND the future: $x_{t+1}, x_{t+2}, \dots, x_{t+w_{future}}; x_{t-1}, \dots, x_{t-w_{past}}$ (up to windows of w_{past}, w_{future})
- EXACTLY the same algo's

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Background: Linear Regression

patient	weight	height
1	27	43
2	43	54
3	54	72
...
N	(25)	??

- express what we don't know (= 'dependent variable')
- as a linear function of what we know (= 'indep. variable(s)')

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Linear Auto Regression:

Time	Packets Sent(t)
1	43
2	54
3	72
...	...
N	??

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Linear Auto Regression:

Time	Packets Sent ($t-1$)	Packets Sent (t)
1	-	43
2	43	54
3	54	72
...
N	25	??

Number of packets sent (t)

Number of packets sent (t-1)

‘lag-plot’

- lag $w=1$
- Dependent variable = # of packets sent ($S[t]$)
- Independent variable = # of packets sent ($S[t-1]$)

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More details:

- Q1: Can it work with window $w>1$?
- A1: YES!

X_t

X_{t-1}

X_{t-2}

eg, $w=2$

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More details:

- Q1: Can it work with window $w>1$?
- A1: YES! (we'll fit a hyper-plane, then!)

X_t

X_{t-1}

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eg, $w=2$

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eg, $w=2$

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More details: DETAILS

- Q1: Can it work with window $w>1$?
- A1: YES! The problem becomes:

$$\mathbf{X}_{[N \times w]} \times \mathbf{a}_{[w \times 1]} = \mathbf{y}_{[N \times 1]}$$

- **OVER-CONSTRAINED**
 - \mathbf{a} is the vector of the regression coefficients
 - \mathbf{X} has the N values of the w indep. variables
 - \mathbf{y} has the N values of the dependent variable

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More details: DETAILS

- $\mathbf{X}_{[N \times w]} \times \mathbf{a}_{[w \times 1]} = \mathbf{y}_{[N \times 1]}$

Ind-var1 Ind-var-w

time

$$\begin{bmatrix} X_{11}, X_{12}, \dots, X_{1w} \\ X_{21}, X_{22}, \dots, X_{2w} \\ \vdots \\ X_{N1}, X_{N2}, \dots, X_{Nw} \end{bmatrix} \times \begin{bmatrix} a_1 \\ a_2 \\ \vdots \\ a_w \end{bmatrix} = \begin{bmatrix} y_1 \\ y_2 \\ \vdots \\ y_N \end{bmatrix}$$

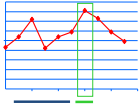
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More details: DETAILS

- $\mathbf{X}_{[N \times w]} \times \mathbf{a}_{[w \times 1]} = \mathbf{y}_{[N \times 1]}$

Ind-var1 Ind-var-w

time

$$\begin{bmatrix} X_{11}, X_{12}, \dots, X_{1w} \\ X_{21}, X_{22}, \dots, X_{2w} \\ \vdots \\ X_{N1}, X_{N2}, \dots, X_{Nw} \end{bmatrix} \times \begin{bmatrix} a_1 \\ a_2 \\ \vdots \\ a_w \end{bmatrix} = \begin{bmatrix} y_1 \\ y_2 \\ \vdots \\ y_N \end{bmatrix}$$


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More details DETAILS

- Q2: How to estimate $a_1, a_2, \dots, a_w = \mathbf{a}$?
- A2: with Least Squares fit

$$\mathbf{a} = (\mathbf{X}^T \times \mathbf{X})^{-1} \times (\mathbf{X}^T \times \mathbf{y})$$

- (Moore-Penrose pseudo-inverse)
- \mathbf{a} is the vector that minimizes the RMSE from \mathbf{y}

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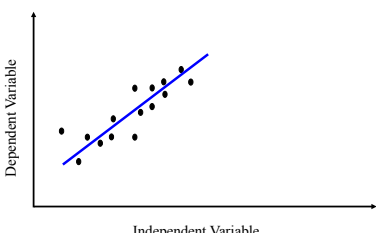
Even more details DETAILS

- Q3: Can we estimate \mathbf{a} incrementally?
- A3: Yes, with the brilliant, classic method of 'Recursive Least Squares' (RLS) (see, e.g., [Yi+00], for details) - pictorially:

[Yi+00] Byoung-Kee Yi et al.: *Online Data Mining for Co-Evolving Time Sequences*, ICDE 2000.

Even more details

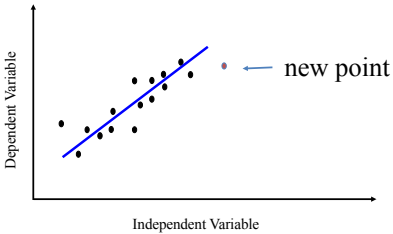
- Given:



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Even more details

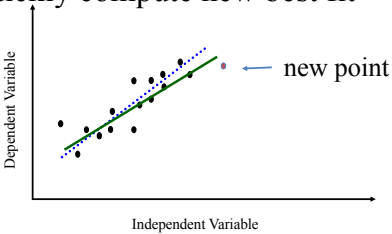
- Given:



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Even more details

Recursive Least Squares (RLS): quickly compute new best fit



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Even more details

- **Straightforward Least Squares**
 - Needs huge matrix (growing in size) $O(N \times w)$
 - Costly matrix operation $O(N \times w^2)$
- **Recursive LS**
 - Need much smaller, fixed size matrix $O(w \times w)$
 - Fast, incremental computation $O(1 \times w^2)$

49,000,000 \longleftrightarrow 49

$N = 10^6, w = 1-100$

http://www.es.kumamoto-u.ac.jp/~yasuko/TALKS/17-KDD-tut/ © 2017 Sakurai, Matsubara & Faloutsos 163

Even more details

- **Straightforward Least Squares**
 - Needs huge matrix (growing in size) $O(N \times w)$
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 - Need much smaller, fixed size matrix $O(w \times w)$
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49,000,000 \longleftrightarrow 49

$N = 10^6, w = 1-100$

RLS: GREAT for streams

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Even more detail DETAILS

- Q4: can we 'forget' the older samples?
- A4: Yes - RLS can easily handle that $[Y_{i+00}]$:

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Adaptability - 'forgetting' DETAILS

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Adaptability - 'forgetting' DETAILS

Trend change

(R)LS with no forgetting

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Adaptability - 'forgetting' DETAILS

Trend change

(R)LS with no forgetting

(R)LS with forgetting

- RLS: can *trivially* handle 'forgetting'

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How to choose 'w'?

- Quick & dirty answer: $w=1$ or $w=2$
- Better answer: Model selection (say, with BIC or MDL – see later)
- Even better answer: **multi-scale windows** [Papadimitriou+, vldb2003]

Spiros Papadimitriou, Anthony Brockwell and Christos Faloutsos *Adaptive, Hands-Off Stream Mining VLDB 2003, Berlin, Germany, Sept. 2003*

How to choose 'w'?

- goal: capture arbitrary periodicities
- with NO human intervention
- on a semi-infinite stream

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Answer:

- 'AWSOM' (Arbitrary Window Stream forecasting Method) [Papadimitriou+, vldb2003]
- idea: do AR on each wavelet level
- in detail:

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AWSOM

The diagram shows a time series x_t on the left. To its right, a grid of plots shows wavelet levels $W_{i,t}$ for $i=1, 2, 3, 4$. Below this, a larger plot shows the decomposition of $W_{2,t}$ into $W_{3,t}$ and $V_{2,t}$. The axes are labeled 'frequency' and 'time'.

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AWSOM

This diagram is similar to the previous one but highlights the relationship between $W_{i,t}$ and $V_{i,t}$ with red circles and arrows, showing how higher-level wavelets are composed of lower-level wavelets and noise.

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AWSOM - idea

The diagram shows a grid of plots for wavelet levels $W_{i,t}$ and $W_{i',t'}$. Arrows indicate the autoregressive relationship between levels. To the right, the equations are given:

$$W_{i,t} = \beta_{i,1}W_{i,t-1} + \beta_{i,2}W_{i,t-2} + \dots$$

$$W_{i',t'} = \beta_{i',1}W_{i',t'-1} + \beta_{i',2}W_{i',t'-2} + \dots$$

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More details...

- Update of wavelet coefficients (incremental)
- Update of linear models (incremental; RLS)
- Feature selection (single-pass)
 - Not all correlations are significant
 - Throw away the insignificant ones (“noise”)

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Results - Synthetic data

- Triangle pulse
- Mix (sine + square)
- AR captures wrong trend (or none)
- Seasonal AR estimation fails

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Results - Real data

- Automobile traffic
 - Daily periodicity
 - Bursty “noise” at smaller scales
- AR fails to capture any trend
- Seasonal AR estimation fails

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Results - real data

- Sunspot intensity
 - Slightly time-varying “period”
- AR captures wrong trend
- Seasonal ARIMA
 - wrong downward trend, despite help by human!

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Complexity

Space: $O(\lg N + mk^2) \approx O(\lg N)$
 Time: $O(k^2) \approx O(1)$

- Where
 - N : number of points (so far)
 - k : number of regression coefficients; fixed
 - m : number of linear models; $O(\lg N)$

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Roadmap

- Motivation
- Similarity Search and Indexing
- Feature extraction
- Streaming pattern discovery
- Linear forecasting
 - Auto-regression: Least Squares; RLS
- ➔ Co-evolving time sequences
- Automatic mining

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Co-Evolving Time Sequences

- Given: A set of **correlated** time sequences
- Forecast **'Repeated(t)'**

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Solution:

Q: what should we do?
A: Least Squares, with

- Dep. Variable: Repeated(t)
- Indep. Variables:
 - Sent(t-1), ..., Sent(t-w);
 - Lost(t-1), ..., Lost(t-w);
 - Repeated(t-1), ...
- (named: 'MUSCLES' [Yi+00])

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Practitioner's guide

- AR(IMA) methodology: prevailing method for linear forecasting
- Brilliant method of Recursive Least Squares for fast, incremental estimation.
- See [Box-Jenkins]

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Resources: software and urls

- MUSCLES: Prof. Byoung-Kee Yi:
<http://www.postech.ac.kr/~bkyi/>
or christos@cs.cmu.edu
- free-ware: 'R' for stat. analysis (clone of Splus)
<http://cran.r-project.org/>

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Books

- George E.P. Box and Gwilym M. Jenkins and Gregory C. Reinsel, *Time Series Analysis: Forecasting and Control*, Prentice Hall, 1994 (the classic book on ARIMA, 3rd ed.)
- Brockwell, P. J. and R. A. Davis (1987). *Time Series: Theory and Methods*. New York, Springer Verlag.

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Additional Reading

- [Papadimitriou+ vldb2003] Spiros Papadimitriou, Anthony Brockwell and Christos Faloutsos *Adaptive, Hands-Off Stream Mining* VLDB 2003, Berlin, Germany, Sept. 2003
- [Yi+00] Byoung-Kee Yi et al.: *Online Data Mining for Co-Evolving Time Sequences*, ICDE 2000. (Describes MUSCLES and Recursive Least Squares)

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Outline

- Motivation
- Similarity Search and Indexing
- Feature extraction
- Linear forecasting
- ➔ Streaming pattern discovery
- Automatic mining

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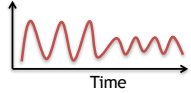
Stream mining

- Applications
 - Sensor monitoring
 - Network analysis
 - Financial and/or business transaction data
 - Web access and media service logs
 - Moving object tracking
 - Industrial manufacturing

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Stream mining

- Requirements
 - **Fast**
high performance and quick response
 - **Nimble**
low memory consumption, single scan
 - **Accurate**
good approximation for pattern discovery and feature extraction



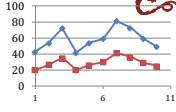
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Monitoring data streams

- Correlation coefficient

$$\rho = \frac{\sum_{i=1}^n (x_i - \bar{x}) \cdot (y_i - \bar{y})}{\sigma(x) \cdot \sigma(y)} \quad \sigma(x) = \sqrt{\sum_{i=1}^n (x_i - \bar{x})^2}$$
- Correlation coefficient and the (Euclidean) distance

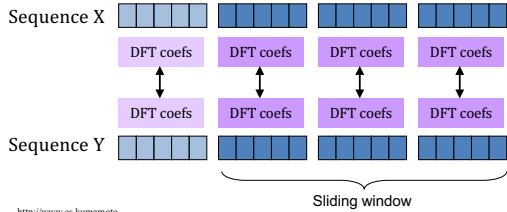
$$\rho = 1 - \frac{1}{2} \sum_{i=1}^n (\hat{x}_i - \hat{y}_i)^2 \quad \hat{x}_i = (x_i - \bar{x}) / \sigma(x)$$



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Monitoring data streams

- Correlation monitoring [Zhu+, vldb02]
 - DFT coefficients for each basic window
 - Correlation coefficient of each sliding window computed from the 'sketch' (DFT coeffs)



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Monitoring data streams

- Grid structure (to avoid checking all pairs)
 - DFT coefficients yields a vector
 - High correlation \rightarrow closeness in the vector space

Vector V_X of sequence X
 Vector V_Y of sequence Y

Correlation coefficients and the Euclidean distance

$$\rho = 1 - \frac{1}{2} \sum_{i=1}^n (\hat{x}_i - \hat{y}_i)^2$$

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Monitoring data streams

- Lag correlation [Sakurai+, sigmod05]

CCF (Cross-Correlation Function)

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Monitoring data streams

- Lag correlation [Sakurai+, sigmod05]

correlated with lag $l=1300$

CCF (Cross-Correlation Function)

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Lag correlation

- Definition of 'score', absolute value of $R(l)$

$$score(l) = |R(l)| \quad R(l) = \frac{\sum_{t=l+1}^n (x_t - \bar{x})(y_{t-l} - \bar{y})}{\sqrt{\sum_{t=l+1}^n (x_t - \bar{x})^2} \sqrt{\sum_{t=1}^{n-l} (y_t - \bar{y})^2}}$$

- Lag correlation
 - Given a threshold γ , $score(l) > \gamma$
 - A local maximum
 - The earliest such maximum, if more maxima exist

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Lag correlation

- Why not naïve?
 - Compute correlation coefficient for each lag
 - $l = \{0, 1, 2, 3, \dots, n/2\}$
- But
 - $O(n)$ space
 - $O(n^2)$ time
 - or $O(n \log n)$ time w/ FFT

Correlation

Lag

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Lag correlation

- BRAID
 - Geometric lag probing + smoothing
 - Use colored windows
 - Keep track of only a geometric progression of the lag values: $l = \{0, 1, 2, 4, 8, \dots, 2^h, \dots\}$

Multi-scale windows

Correlation

Lag

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Lag correlation

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Lag correlation

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Lag correlation

- BRAID
 - Geometric lag probing + smoothing
 - Keep track of only a geometric progression of the lag values: $l = \{0, 1, 2, 4, 8, \dots, 2^h, \dots\}$

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Lag correlation

- BRAID
 - Geometric lag probing + smoothing
 - Keep track of only a geometric progression of the lag values: $l = \{0, 1, 2, 4, 8, \dots, 2^h, \dots\}$
 - Use a cubic spline to interpolate

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Lag correlation

- Why not naïve?
 - Compute correlation coefficient for each lag
 - $l = \{0, 1, 2, 3, \dots, n/2\}$
- But
 - $O(n)$ space
 - $O(n^2)$ time
 - or $O(n \log n)$ time w/ l

BRAID

- $O(\log n)$ space
- $O(l)$ time

Multi-scale windows

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BRAID in the real world

- Bridge structural health monitoring
 - Structural monitoring using vibration/shock sensors
 - Keep track of lag correlations for sensor data streams

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BRAID in the real world

- Bridge structural health monitoring
 - Goal: real-time anomaly detection for disaster prevention
 - Several thousands readings (per sec) from several hundreds sensor nodes
- Uses BRAID
- Metropolitan Expressway (Tokyo, Japan)

Structural health monitoring

Vibration/shock sensor

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BRAID in the real world

- Bridge structural health monitoring with BRAID

Metropolitan Expressway (Tokyo, Japan)

Can Tho Bridge (Vietnam)

Tokyo Gate Bridge (Tokyo, Japan)

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Feature extraction from streams

- Find hidden variables from streams [Papadimitriou+, vldb2005]

major leak

normal operation

water distribution network

May have hundreds of measurements, but it is **unlikely they are completely unrelated!**

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Feature extraction from streams

hidden variables

Phase 1 Phase 2 Phase 3

chlorine concentrations

sensors near leak

sensors away from leak

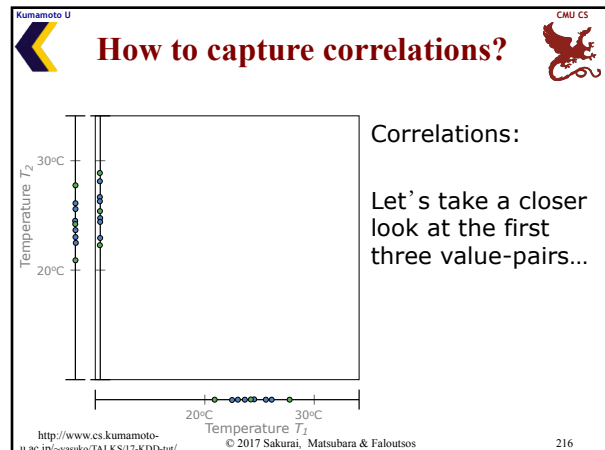
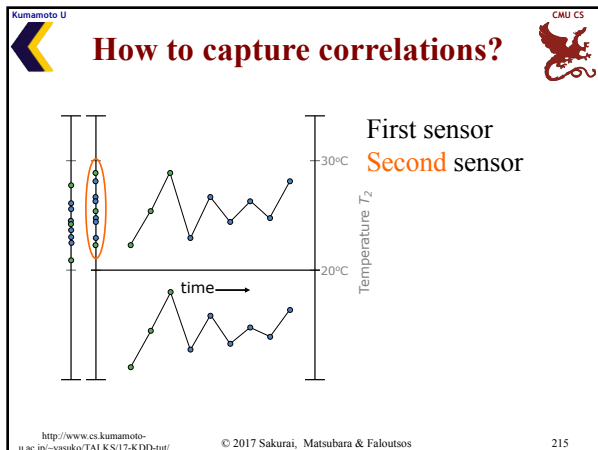
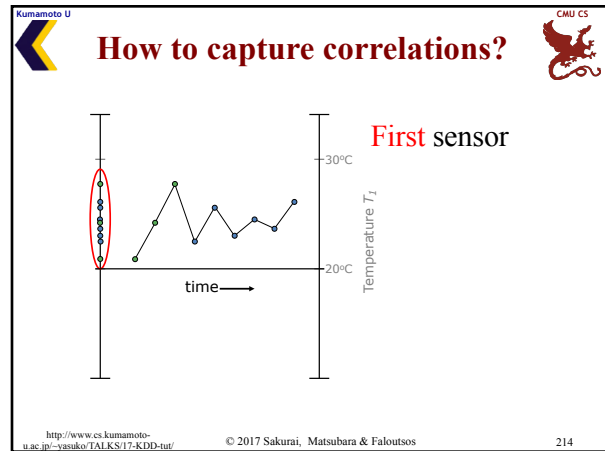
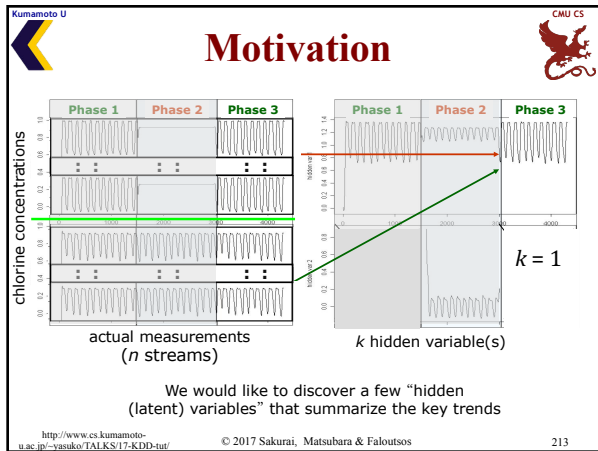
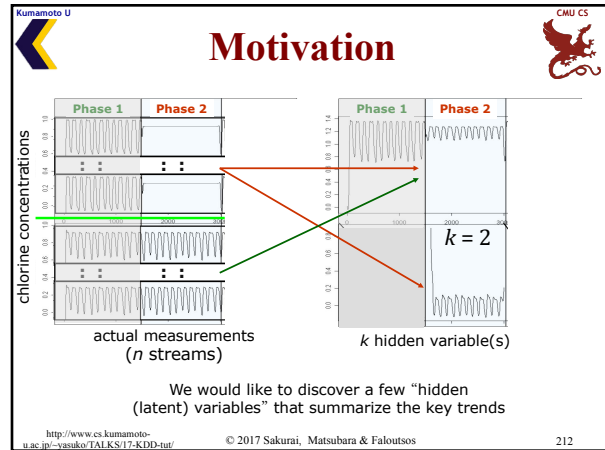
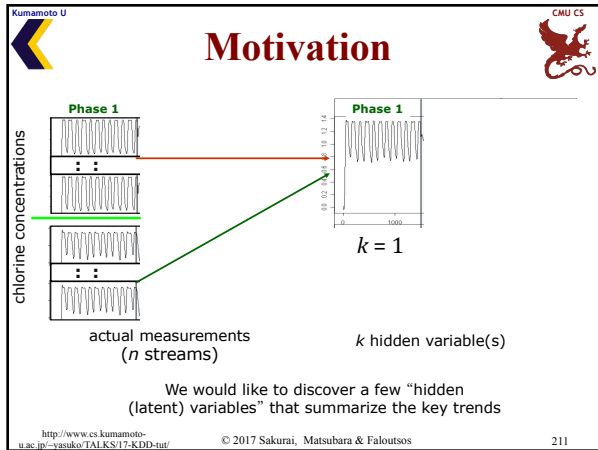
water distribution network

normal operation

major leak

May have hundreds of measurements, but it is **unlikely they are completely unrelated!**

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How to capture correlations?

First three lie (almost) on a line in the space of value-pairs...

- $O(n)$ numbers for the slope, and
- *One* number for each value-pair (offset on line)

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How to capture correlations?

Other pairs also follow the same pattern: they lie (approximately) on this line

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Incremental update

For each new point

- Project onto current line
- Estimate error

• New value

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Incremental update

For each new point

- Project onto current line
- Estimate error
- Rotate line in the direction of the error and in proportion to its magnitude

→ $O(n)$ time

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Incremental update

For each new point

- Project onto current line
- Estimate error
- Rotate line in the direction of the error and in proportion to its magnitude

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Related work

- Wavelet over streams [Gilbert+, vldb01] [Guha+, vldb04]
- Fourier representations [Gilbert+, stoc02]
- KNN [Koudas+, 04] [Korn+, vldb02]
- Histograms [Guha+, stoc01]
- Clustering [Guha+, focs00] [Aggarwal+, vldb03]
- Sketches [Indyk+, vldb00] [Cormode+, J. Algorithms 05]
- ...
- ...

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Related work

- Heavy hitters [Cormode+, vldb03]
- Data embedding [Indyk+, focs00]
- Burst detection [Zhu+, kdd03]
- Segmentation [Keogh+, icdm01]
- Multiple scale analysis [Papadimitriou+, sigmod06]
- Fractal [Korn+, sigmod06]
- Time warping [Sakurai+, icde07]...
- ...

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Outline

- Motivation
- Similarity Search and Indexing
- Feature extraction
- Streaming pattern discovery
- Linear forecasting
- ➔ Automatic mining

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Motivation

Given: co-evolving time-series
 – e.g., MoCap (leg/arm sensors)

“Chicken dance”

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Motivation

Given: co-evolving time-series
 – e.g., MoCap (leg/arm sensors)

“Chicken dance”

Q. Any distinct patterns?

Q. If yes, how many?

Q. What kind?

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Motivation

Challenges: co-evolving sequences

- Unknown # of patterns (e.g., beaks)
- Different durations

beaks wings tail feathers claps

left/right legs 1

left/right arms 0.5

Time

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Motivation

Goal: find patterns that agree with human intuition

Input

left/right legs 1

left/right arms 0.5

Time

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Motivation

Goal: find patterns that agree with human intuition

Input: left/right legs, left/right arms

Output: Beaks, Tail feathers, Claps, Wings

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Motivation

Goal: find patterns that agree with human intuition

Input: left/right legs, left/right arms

NO magic numbers!

Automatic!

Output: Beaks, Tail feathers, Claps, Wings

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Why: Automatic mining

No magic numbers! ... because,

Manual (use magic)

- sensitive to the parameter tuning
- long tuning steps (hours, days, ...)

Automatic (no magic numbers)

- no expert tuning required

Big data mining:
-> we cannot afford human intervention!!

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How: Automatic mining

Goal: fully-automatic modeling

- Given: **data X**
- Find: a compact description (**model M**) of X

Q. How can we find the best model M?

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How: Automatic mining

Goal: fully-automatic modeling

- Given: **data X**
- Find: a compact description (**model M**) of X

Answer: MDL!

Q. How can we find the best model M?

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Solution: MDL (Minimum description length)

Solution: Minimize total encoding cost \$!

- Occam's razor (i.e., law of parsimony)
- **Fully automatic** parameter optimization
- No over-fitting

Ideal model

[Bishop: PR&ML]

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Solution: MDL (Minimum description length)

Solution: Minimize total encoding cost \$!

$$\text{Cost}_T(X;M) = \min (\text{Cost}_M(M) + \text{Cost}_c(X|M))$$

Total cost **Model cost** **Coding cost (error)**

\$\$\$ \$\$ \$ (Ideal!) \$\$\$\$

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[Matsubara+ SIGMOD'14]

AutoPlait: Automatic Mining of Co-evolving Time Sequences

Yasuko Matsubara (Kumamoto University)
Yasushi Sakurai (Kumamoto University),
Christos Faloutsos (CMU)

http://www.es.kumamoto-u.ac.jp/~yasuko/TALKS/17-KDD-tut/ © 2017 Sakurai, Matsubara & Faloutsos 236

Problem definition

Goal: find patterns that agree with human intuition

Input

Output

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Problem definition

- Bundle** : set of d co-evolving sequences

given $X = \{x_1, \dots, x_n\}$
 $d \times n$

Bundle X ($d=4$)

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Problem definition

- Segment**: convert $X \rightarrow m$ segments, S

hidden $S = \{s_1, \dots, s_m\}$

Segment ($m=8$)

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Problem definition

- Regime**: segment groups: $\Theta = \{\theta_1, \theta_2, \dots, \theta_r, \Delta_{r \times r}\}$

hidden θ_r : model of regime r

Regimes ($r=4$)

beaks θ_1
wings θ_2
 θ_3
 θ_4

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Problem definition

- Segment-membership: assignment

hidden $F = \{f_1, \dots, f_m\}$

$F = \{ \begin{matrix} 1 & 2 & 4 & 1 & 3 & 2 & 4 & 1 & 3 \\ 0.5 & & & & & & & & \\ 0 & & & & & & & & \end{matrix} \}$

Segment-membership (m=8)

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Problem definition

- Given: bundle X

$X = \{x_1, \dots, x_n\}$

- Find: compact description C of X

$C = \{m, r, S, \Theta, F\}$

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Problem definition

- Given: bundle X

$X = \{x_1, \dots, x_n\}$

- Find: compact description C of X

$C = \{m, r, S, \Theta, F\}$

m segments
r regimes
Segment-membership

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Main ideas

Goal: compact description of X

$C = \{m, r, S, \Theta, F\}$

without user intervention!!

Challenges:

Q1. How to generate 'informative' regimes ?

Q2. How to decide # of regimes/segments ?

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Main ideas

Goal: compact description of X

$C = \{m, r, S, \Theta, F\}$

without user intervention!!

Challenges:

Q1. How to generate 'informative' regimes ?

Idea (1): Multi-level chain model

Q2. How to decide # of regimes/segments ?

Idea (2): Model description cost

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Idea (1): MLCM: multi-level chain model

Q1. How to generate 'informative' regimes ?

Sequences \rightarrow Model \rightarrow Regimes

beaks, claps, wings

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Idea (1): MLCM: multi-level chain model

Q1. How to generate 'informative' regimes?

Sequences → Model → Regimes

Idea (1): Multi-level chain model

- HMM-based probabilistic model
- with "across-regime" transitions

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Idea (1): MLCM: multi-level chain model

$\Theta = \{\theta_1, \theta_2, \dots, \theta_r, \Delta_{r \times r}\}$ ($\theta_i = \{\pi, A, B\}$)

r regimes (HMMs) across-regime transition prob. Single HMM parameters

Regimes $r=2$
Regime 1 ($k=3$)
Regime 2 ($k=2$)

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Idea (2): model description cost

Q2. How to decide # of regimes/segments?

Idea (2): Model description cost

- Minimize encoding cost
- find "optimal" # of segments/regimes

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Idea (2): model description cost

Idea: Minimize encoding cost!

$\min (\text{Cost}_M(M) + \text{Cost}_C(X|M))$

Model cost Coding cost

Good compression ↔ Good description

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Idea (2): model description cost

Total cost of bundle X, given C

$C = \{m, r, S, \Theta, F\}$

$$\text{Cost}_T(\mathbf{X}; C) = \text{Cost}_T(\mathbf{X}; m, r, S, \Theta, F)$$

$$= \log^*(n) + \log^*(d) + \log^*(m) + \log^*(r) + m \log(r) + \sum_{i=1}^{m-1} \log^* |s_i| + \text{Cost}_M(\Theta) + \text{Cost}_C(\mathbf{X}|\Theta) \quad (6)$$

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Idea (2): model description cost

Total cost of bundle X, given C

$C = \{m, r, S, \Theta, F\}$

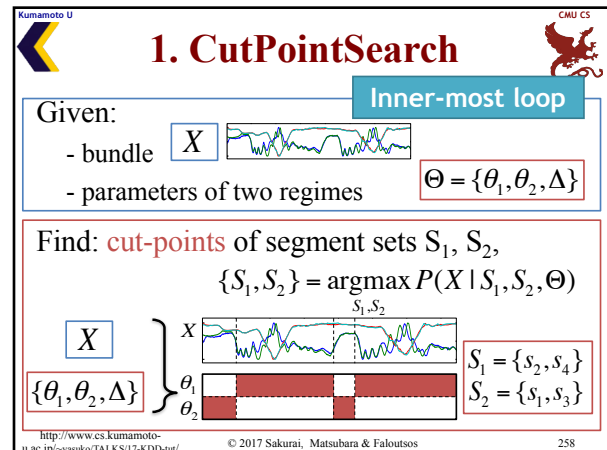
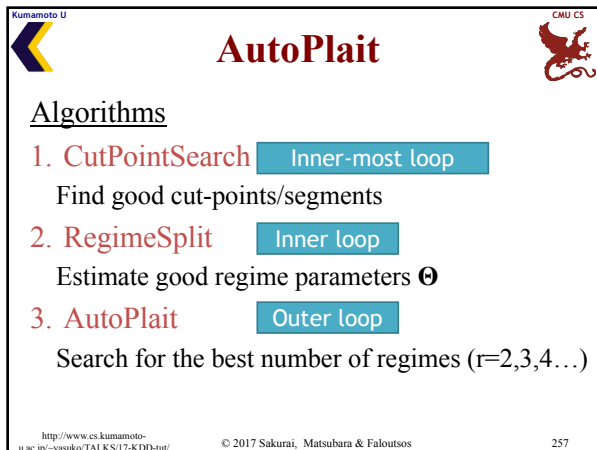
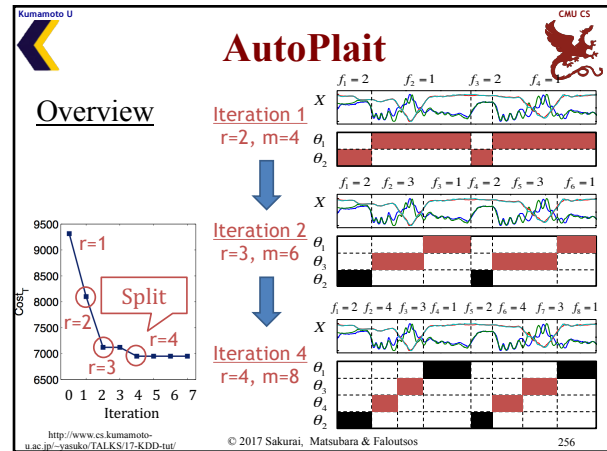
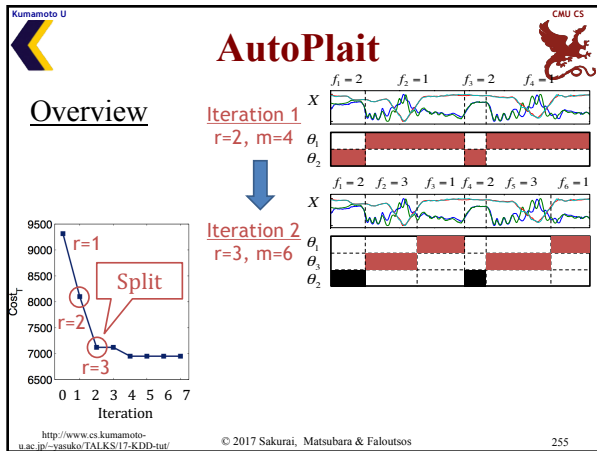
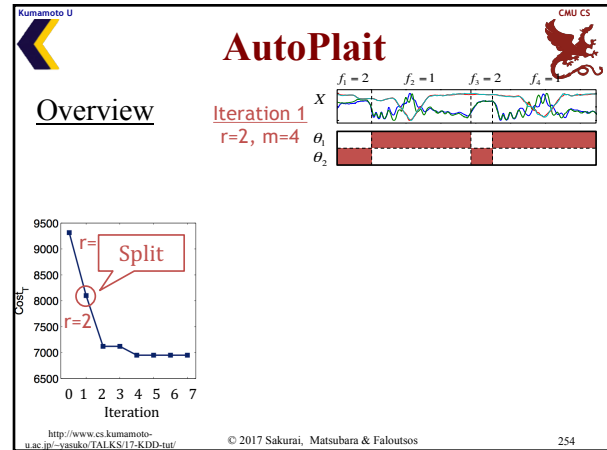
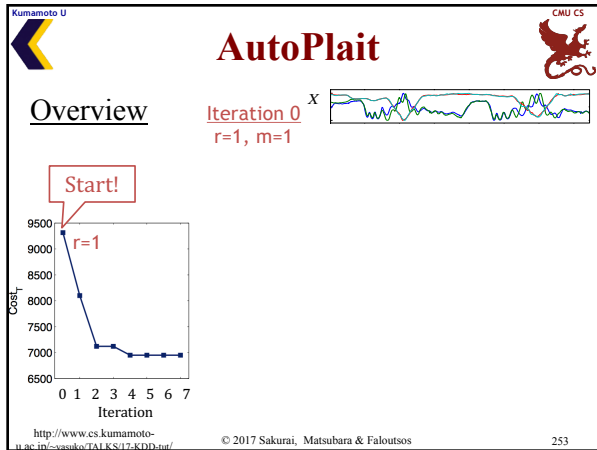
duration/dimensions # of segments/regime membership F

$$\text{Cost}_T(\mathbf{X}; C) = \text{Cost}_T(\mathbf{X}; m, r, S, \Theta, F)$$

$$= \log^*(n) + \log^*(d) + \log^*(m) + \log^*(r) + m \log(r) + \sum_{i=1}^{m-1} \log^* |s_i| + \text{Cost}_M(\Theta) + \text{Cost}_C(\mathbf{X}|\Theta) \quad (6)$$

segment lengths Model description cost Coding cost of X given Θ

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1. CutPointSearch

DP algorithm to compute likelihood: $P(X|\Theta)$

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1. CutPointSearch

Theoretical analysis

Scalability

- It takes $O(ndk^2)$ time (only single scan)
- n: length of X
- d: dimension of X
- k: # of hidden states in regime

Accuracy

It guarantees the optimal cut points

- (Details in paper)

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2. RegimeSplit

Given: bundle X

Find: two regimes

1. find cut-points of segment sets: S_1, S_2
2. estimate parameters of two regimes: $\Theta = \{\theta_1, \theta_2, \Delta\}$

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2. RegimeSplit

Two-phase iterative approach

- Phase 1: (CutPointSearch)
- Split segments into two groups: S_1, S_2
- Phase 2: (BaumWelch)
- Update model parameters: $\Theta = \{\theta_1, \theta_2, \Delta\}$

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3. AutoPlait

Given: bundle X

Find: r regimes (r=2, 3, 4, ...)

- i.e., find full parameter set $C = \{m, r, S, \Theta, F\}$

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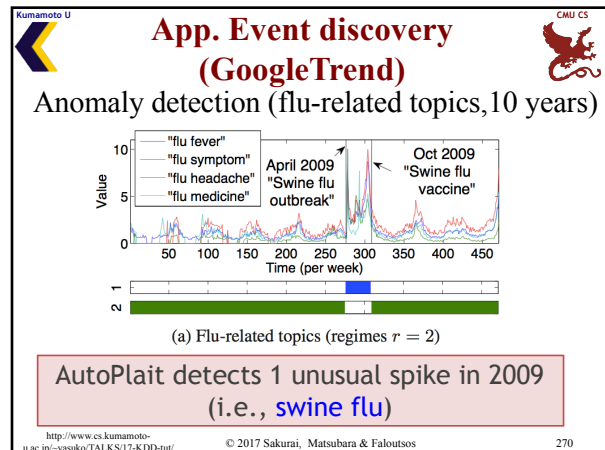
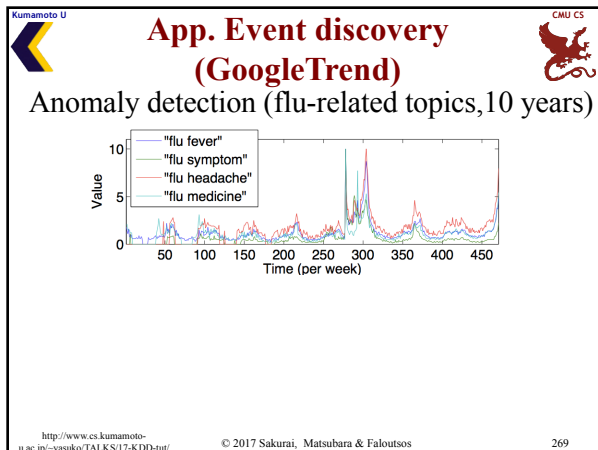
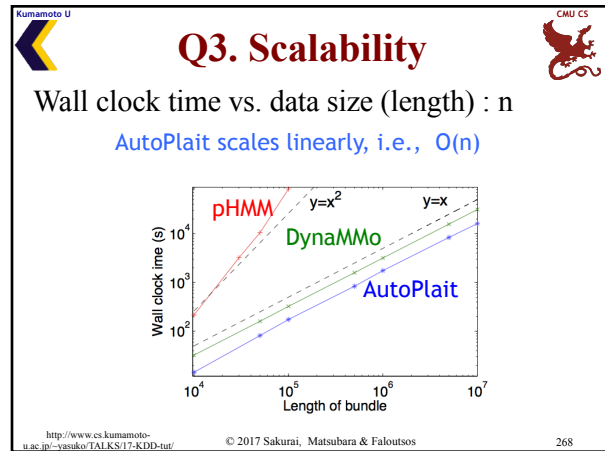
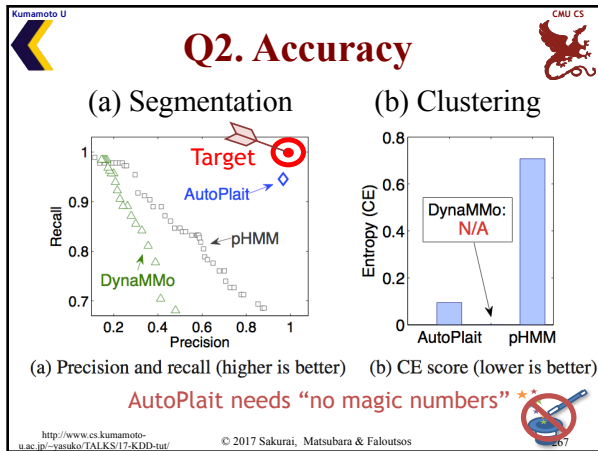
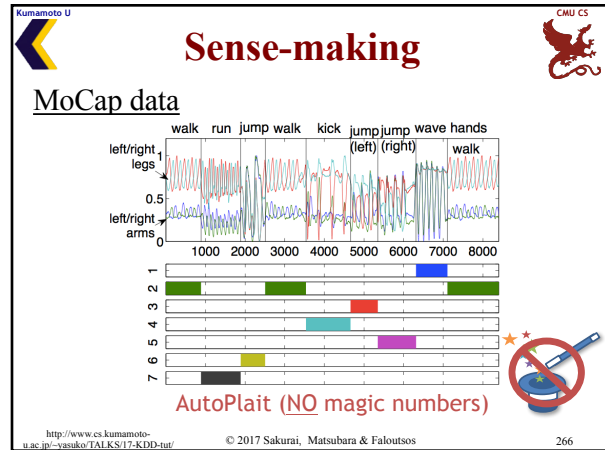
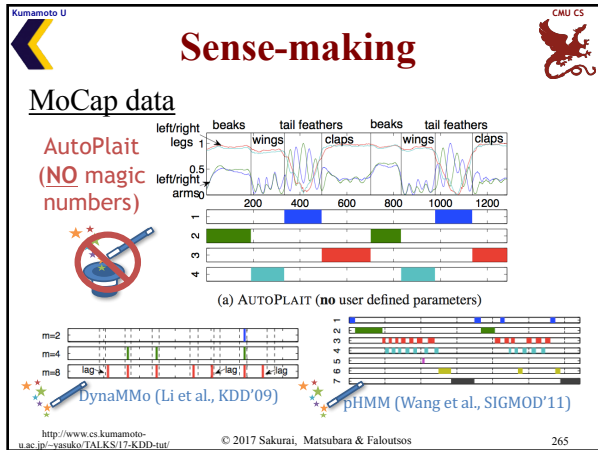
3. AutoPlait

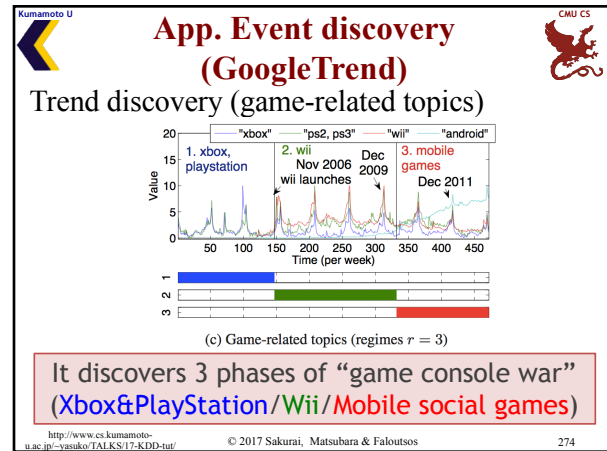
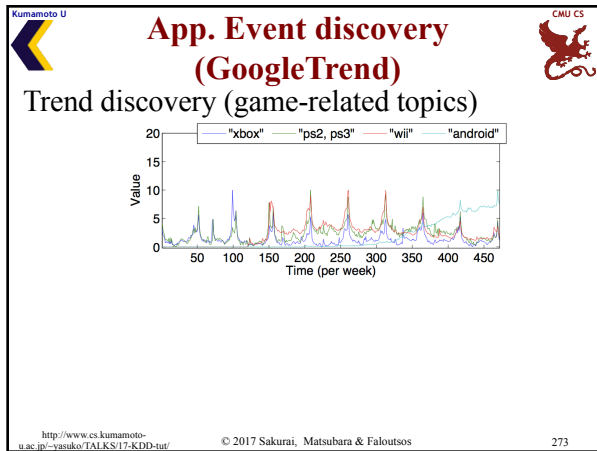
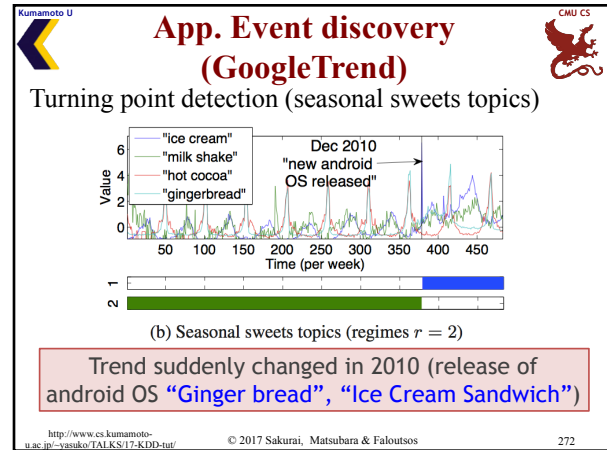
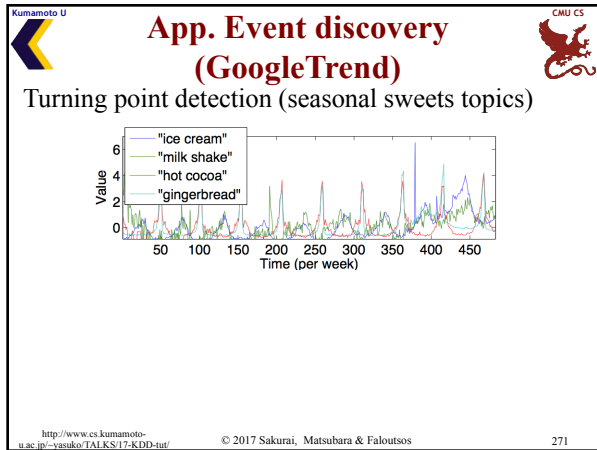
Split regimes $r=2, 3, \dots$, as long as cost keeps decreasing

- Find appropriate # of regimes

$r = \min_r Cost_T(X; m, r, S, \Theta, F)$

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Industrial contribution

- Automobile sensor data
 - location, velocity, longitudinal/lateral acceleration


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Code at

- <http://www.cs.kumamoto-u.ac.jp/~yasuko/software.html>


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Part 1 – Conclusions

- Motivation
- Similarity Search and Indexing
- Feature extraction
- Linear forecasting
- Streaming pattern discovery
- Automatic mining


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Part 1 – Conclusions

- Motivation
- Similarity Search and Indexing
 - Euclidean/time-warping
 - extract features
 - index (SAM, R-tree)
- Feature extraction
 - SVD, ICA, DFT, DWT (multi-scale windows)


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Part 1 – Conclusions

- Linear forecasting
 - AR, RLS
- Streaming pattern discovery
 - RLS, “incremental” wavelet transform
 - Multi-scale windows
- Automatic mining
 - MDL


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Part 1

Similarity search, pattern discovery and summarization

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